
Codex Africanus Documentation

Release 0.1.5

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CHAPTER 1

Codex Africanus

Radio Astronomy Building Blocks

1.1 Documentation

<https://codex-africanus.readthedocs.io>.

2.1 Stable release

To install Codex Africanus, run this command in your terminal:

```
$ pip install codex-africanus
```

This is the preferred method to install Codex Africanus, as it will always install the most recent stable release.

If you don't have [pip](#) installed, this [Python installation guide](#) can guide you through the process.

By default, Codex Africanus will install with a minimal set of dependencies, numpy and numba.

Further functionality can be enabled by installing extra requirements as follows:

```
$ pip install codex-africanus[dask]
$ pip install codex-africanus[scipy]
$ pip install codex-africanus[astropy]
$ pip install codex-africanus[python-casacore]
```

To install the complete set of dependencies for the CPU:

```
$ pip install codex-africanus[complete]
```

To install the complete set of dependencies including CUDA:

```
$ pip install codex-africanus[complete-cuda]
```

2.2 From sources

The sources for Codex Africanus can be downloaded from the [Github repo](#).

You can either clone the public repository:

```
$ git clone git://github.com/ska-sa/codex-africanus
```

Or download the [tarball](#):

```
$ curl -OL https://github.com/ska-sa/codex-africanus/tarball/master
```

Once you have a copy of the source, you can install it with:

```
$ python setup.py install
```


CHAPTER 3

Usage

To use Codex Africanus in a project:

```
import africanus
```

Command Line Utilities

The following command line utilities are installed. Run each utility's help for further information.

```
$ utility --help
```

4.1 plot-filter

Plots convolution filters.

4.2 plot-taper

Plots tapers associated with convolution filters.

5.1 Radio Interferometer Measurement Equation

Functions used to compute the terms of the Radio Interferometer Measurement Equation (RIME). It describes the response of an interferometer to a sky model.

$$V_{pq} = G_p \left(\sum_s E_{ps} L_p K_{ps} B_s K_{qs}^H L_q^H E_{qs}^H \right) G_q^H$$

where for antenna p and q , and source s :

- G_p represents direction-independent effects.
- E_{ps} represents direction-dependent effects.
- L_p represents the feed rotation.
- K_{ps} represents the phase delay term.
- B_s represents the brightness matrix.

The RIME is more formally described in the following four papers:

- I. A full-sky Jones formalism
- II. Calibration and direction-dependent effects
- III. Addressing direction-dependent effects in 21cm WSRT observations of 3C147
- IV. A generalized tensor formalism

5.1.1 Numpy

<code>predict_vis</code> (time_index, antenna1, antenna2)	Multiply Jones terms together to form model visibilities according to the following formula:
<code>phase_delay</code> (lm, uvw, frequency)	Computes the phase delay (K) term:
<code>parallactic_angles</code> (times, antenna_positions, ...)	Computes parallactic angles per timestep for the given reference antenna position and field centre.
<code>feed_rotation</code> (parallactic_angles[, feed_type])	Computes the 2x2 feed rotation (L) matrix from the parallactic_angles.
<code>transform_sources</code> (lm, parallactic_angles, ...)	Creates beam sampling coordinates suitable for use in <code>beam_cube_dde()</code> by:
<code>beam_cube_dde</code> (beam, coords, l_grid, m_grid, ...)	Computes Direction Dependent Effects (E) by sampling complex values in <code>beam</code> at the coordinates <code>coords</code> .
<code>zernike_dde</code> (coords, coeffs, noll_index)	Computes Direction Dependent Effects by evaluating Zernicke Polynomials defined by coefficients <code>coeffs</code> and noll indexes <code>noll_index</code> at the specified coordinates <code>coords</code> .

```
africanus.rime.predict_vis (time_index,      antenna1,      antenna2,      dde1_jones=None,
                             source_coh=None,      dde2_jones=None,      die1_jones=None,
                             base_vis=None, die2_jones=None)
```

Multiply Jones terms together to form model visibilities according to the following formula:

$$V_{pq} = G_p \left(B_{pq} + \sum_s A_{ps} X_{pqs} A_{qs}^H \right) G_q^H$$

where for antenna p and q , and source s :

- B_{pq} represent base coherencies.
- E_{ps} represents Direction-Dependent Jones terms.
- X_{pqs} represents a coherency matrix (per-source).
- G_p represents Direction-Independent Jones terms.

Generally, E_{ps} , G_p , X_{pqs} should be formed by using the [RIME API](#) functions and combining them together with `einsum()`.

Please read the Notes

Parameters

time_index [[numpy.ndarray](#)] Time index used to look up the antenna Jones index for a particular baseline. shape (row,).

antenna1 [[numpy.ndarray](#)] Antenna 1 index used to look up the antenna Jones for a particular baseline. with shape (row,).

antenna2 [[numpy.ndarray](#)] Antenna 2 index used to look up the antenna Jones for a particular baseline. with shape (row,).

dde1_jones [[numpy.ndarray](#), optional] A_{ps} Direction-Dependent Jones terms for the first antenna. shape (source, time, ant, chan, corr_1, corr_2)

source_coh [[numpy.ndarray](#), optional] X_{pqs} Direction-Dependent Coherency matrix for the baseline. with shape (source, row, chan, corr_1, corr_2)

dde2_jones [[numpy.ndarray](#), optional] A_{qs} Direction-Dependent Jones terms for the second antenna. shape (source, time, ant, chan, corr_1, corr_2)

die1_jones [numpy.ndarray, optional] G_{ps} Direction-Independent Jones terms for the first antenna of the baseline. with shape (time, ant, chan, corr_1, corr_2)

base_vis [numpy.ndarray, optional] B_{pq} base visibilities, added to source coherency summation *before* multiplication with *die1_jones* and *die2_jones*.

die2_jones [numpy.ndarray, optional] G_{ps} Direction-Independent Jones terms for the second antenna of the baseline. with shape (time, ant, chan, corr_1, corr_2)

Returns

visibilities [numpy.ndarray] Model visibilities of shape (row, chan, corr_1, corr_2)

Notes

- Direction-Dependent terms (dde{1,2}_jones) and Independent (die{1,2}_jones) are optional, but if one is present, the other must be present.
- The inputs to this function involve row, time and ant (antenna) dimensions.
- Each row is associated with a pair of antenna Jones matrices at a particular timestep via the time_index, antennal and antenna2 inputs.
- The row dimension must be an increasing partial order in time.

africanus.rime.**phase_delay**(lm, uvw, frequency)

Computes the phase delay (K) term:

$$e^{-2\pi i(ul+vm+w(n-1))}$$

where $n = \sqrt{1 - l^2 - m^2}$

Parameters

lm [numpy.ndarray] LM coordinates of shape (source, 2) with L and M components in the last dimension.

uvw [numpy.ndarray] UVW coordinates of shape (row, 3) with U, V and W components in the last dimension.

frequency [numpy.ndarray] frequencies of shape (chan,)

Returns

complex_phase [numpy.ndarray] complex of shape (source, row, chan)

Notes

Corresponds to the complex exponential of the [Van Cittert-Zernike Theorem](#).

[MeqTrees](#) uses a positive sign convention and so any UVW coordinates must be inverted in order for their phase delay terms (and therefore visibilities) to agree.

africanus.rime.**parallactic_angles**(times, antenna_positions, field_centre, backend='casa')

Computes parallactic angles per timestep for the given reference antenna position and field centre.

Parameters

times [numpy.ndarray] Array of Mean Julian Date times in *seconds* with shape (time,),

antenna_positions [`numpy.ndarray`] Antenna positions of shape `(ant, 3)` in *metres* in the *ITRF* frame.

field_centre [`numpy.ndarray`] Field centre of shape `(2,)` in *radians*

backend [`{'casa', 'test'}`, optional] Backend to use for calculating the parallactic angles.

- `casa` defers to an implementation depending on `python-casacore`. This backend should be used by default.
- `test` creates parallactic angles by multiplying the `times` and `antenna_position` arrays. It exist solely for testing.

Returns

parallactic_angles [`numpy.ndarray`] Parallactic angles of shape `(time, ant)`

`africanus.rime.feed_rotation(parallactic_angles, feed_type='linear')`

Computes the 2x2 feed rotation (L) matrix from the `parallactic_angles`.

$$\text{linear} \begin{bmatrix} \cos(pa) & \sin(pa) \\ -\sin(pa) & \cos(pa) \end{bmatrix} \quad \text{circular} \begin{bmatrix} e^{-ipa} & 0 \\ 0 & e^{ipa} \end{bmatrix}$$

Parameters

parallactic_angles [`numpy.ndarray`] floating point parallactic angles. Of shape `(pa0, pa1, ..., pan)`.

feed_type [`{'linear', 'circular'}`] The type of feed

Returns

feed_matrix [`numpy.ndarray`] Feed rotation matrix of shape `(pa0, pa1, ..., pan, 2, 2)`

`africanus.rime.transform_sources(lm, parallactic_angles, pointing_errors, antenna_scaling, frequency, dtype=None)`

Creates beam sampling coordinates suitable for use in `beam_cube_dde()` by:

1. Rotating `lm` coordinates by the `parallactic_angles`
2. Adding `pointing_errors`
3. Scaling by `antenna_scaling`

Parameters

lm [`numpy.ndarray`] LM coordinates of shape `(src, 2)` in radians offset from the phase centre.

parallactic_angles [`numpy.ndarray`] parallactic angles of shape `(time, antenna)` in radians.

pointing_errors [`numpy.ndarray`] LM pointing errors for each antenna at each timestep in radians. Has shape `(time, antenna, 2)`

antenna_scaling [`numpy.ndarray`] antenna scaling factor for each channel and each antenna. Has shape `(antenna, chan)`

frequency [`numpy.ndarray`] frequencies for each channel. Has shape `(chan,)`

dtype [`numpy.dtype`, optional] Numpy dtype of result array. Should be `float32` or `float64`. Defaults to `float64`

Returns

coords [numpy.ndarray] coordinates of shape (3, src, time, antenna, chan) where each coordinate component represents **l**, **m** and **frequency**, respectively.

`africanus.rime.beam_cube_dde`(beam, coords, l_grid, m_grid, freq_grid, spline_order=1, mode='nearest')

Computes Direction Dependent Effects (E) by sampling complex values in beam at the coordinates coords.

Both real and imaginary beam values are sampled at the given coordinates and normalised to form a **mean of circular quantities**.

`l_grid`, `m_grid` and `freq_grid` can be obtained from `beam_grids()`.

Parameters

beam [numpy.ndarray] complex beam cube of shape (beam_lw, beam_mh, beam_nud, corr_1, corr_2) where beam_lw is the grid width of the l dimension, beam_mh is the grid height of the m dimension and beam_nud is the grid depth of the frequency dimension. Either corr_1 or both corr_1 and corr_2 may be present, representing 1, 2 or 2x2 correlations respectively.

coords [numpy.ndarray] beam cube coordinates of shape (coords, dim_1, ..., dim_n) where coord always has size 3 and refers to (l,m,frequency).

l_grid [numpy.ndarray] Monotonically *increasing* or *decreasing* grid values for the l axis, with shape (beam_lw,). If decreasing, the

m_grid [numpy.ndarray] Monotonically *increasing* or *decreasing* grid values for the m axis, with shape (beam_mh,)

freq_grid [numpy.ndarray] Monotonically increasing grid values for the frequency axis, with shape (beam_nud,)

spline_order [int] Spline order to use in `scipy.ndimage.interpolation.map_coordinates()`. Defaults to 1 ('linear')

mode [str] Border mode to use in `scipy.ndimage.interpolation.map_coordinates()` Defaults to 'nearest'

Returns

dde [numpy.ndarray] Sampled complex beam values at the specified coordinates with shape (dim_1, ..., dim_n, corr_1, corr_2)

`africanus.rime.zernike_dde`(coords, coeffs, noll_index)

Computes Direction Dependent Effects by evaluating **Zernicke Polynomials** defined by coefficients coeffs and noll indexes noll_index at the specified coordinates coords.

Decomposition of a voxel beam cube into Zernicke polynomial coefficients can be achieved through the use of the **eidos** package.

Parameters

coords [numpy.ndarray] Float coordinates at which to evaluate the zernike polynomials. Has shape (3, source, time, ant, chan). The three components in the first dimension represent l, m and frequency coordinates, respectively.

coeffs [numpy.ndarray] complex Zernicke polynomial coefficients. Has shape (ant, chan, corr_1, ..., corr_n, poly) where poly is the number of polynomial coefficients and corr_1, ..., corr_n are a variable number of correlation dimensions.

noll_index [numpy.ndarray] Noll index associated with each polynomial coefficient. Has shape (ant, chan, corr_1, ..., corr_n, poly).

Returns

dde [numpy.ndarray] complex values with shape (source, time, ant, chan, corr_1, ..., corr_n)

5.1.2 Cuda

<code>predict_vis(time_index, antenna1, antenna2, ...)</code>	Multiply Jones terms together to form model visibilities according to the following formula:
<code>phase_delay(lm, uvw, frequency)</code>	Computes the phase delay (K) term:
<code>feed_rotation(parallactic_angles[, feed_type])</code>	Computes the 2x2 feed rotation (L) matrix from the parallactic_angles.

`africanus.rime.cuda.predict_vis` (*time_index*, *antenna1*, *antenna2*, *dde1_jones*, *source_coh*, *dde2_jones*, *die1_jones*, *base_vis*, *die2_jones*)

Multiply Jones terms together to form model visibilities according to the following formula:

$$V_{pq} = G_p \left(B_{pq} + \sum_s A_{ps} X_{pqs} A_{qs}^H \right) G_q^H$$

where for antenna p and q , and source s :

- B_{pq} represent base coherencies.
- E_{ps} represents Direction-Dependent Jones terms.
- X_{pqs} represents a coherency matrix (per-source).
- G_p represents Direction-Independent Jones terms.

Generally, E_{ps} , G_p , X_{pqs} should be formed by using the [RIME API](#) functions and combining them together with `einsum()`.

Please read the Notes**Parameters**

time_index [cupy.ndarray] Time index used to look up the antenna Jones index for a particular baseline. shape (row,).

antenna1 [cupy.ndarray] Antenna 1 index used to look up the antenna Jones for a particular baseline. with shape (row,).

antenna2 [cupy.ndarray] Antenna 2 index used to look up the antenna Jones for a particular baseline. with shape (row,).

dde1_jones [cupy.ndarray, optional] A_{ps} Direction-Dependent Jones terms for the first antenna. shape (source, time, ant, chan, corr_1, corr_2)

source_coh [cupy.ndarray, optional] X_{pqs} Direction-Dependent Coherency matrix for the baseline. with shape (source, row, chan, corr_1, corr_2)

dde2_jones [cupy.ndarray, optional] A_{qs} Direction-Dependent Jones terms for the second antenna. shape (source, time, ant, chan, corr_1, corr_2)

die1_jones [cupy.ndarray, optional] G_{ps} Direction-Independent Jones terms for the first antenna of the baseline. with shape (time, ant, chan, corr_1, corr_2)

base_vis [cupy.ndarray, optional] B_{pq} base visibilities, added to source coherency summation *before* multiplication with *die1_jones* and *die2_jones*.

die2_jones [`cupy.ndarray`, optional] G_{ps} Direction-Independent Jones terms for the second antenna of the baseline. with shape `(time, ant, chan, corr_1, corr_2)`

Returns

visibilities [`cupy.ndarray`] Model visibilities of shape `(row, chan, corr_1, corr_2)`

Notes

- Direction-Dependent terms (`dde{1,2}_jones`) and Independent (`die{1,2}_jones`) are optional, but if one is present, the other must be present.
- The inputs to this function involve `row`, `time` and `ant` (antenna) dimensions.
- Each `row` is associated with a pair of antenna Jones matrices at a particular timestep via the `time_index`, `antenna1` and `antenna2` inputs.
- The `row` dimension must be an increasing partial order in time.

`africanus.rime.cuda.phase_delay(lm, uvw, frequency)`

Computes the phase delay (K) term:

$$e^{-2\pi i(ul+vm+w(n-1))}$$

$$\text{where } n = \sqrt{1 - l^2 - m^2}$$

Parameters

lm [`cupy.ndarray`] LM coordinates of shape `(source, 2)` with L and M components in the last dimension.

uvw [`cupy.ndarray`] UVW coordinates of shape `(row, 3)` with U, V and W components in the last dimension.

frequency [`cupy.ndarray`] frequencies of shape `(chan,)`

Returns

complex_phase [`cupy.ndarray`] complex of shape `(source, row, chan)`

Notes

Corresponds to the complex exponential of the [Van Cittert-Zernike Theorem](#).

[MeqTrees](#) uses a positive sign convention and so any UVW coordinates must be inverted in order for their phase delay terms (and therefore visibilities) to agree.

`africanus.rime.cuda.feed_rotation(parallactic_angles, feed_type='linear')`

Computes the 2x2 feed rotation (L) matrix from the `parallactic_angles`.

$$\text{linear} \begin{bmatrix} \cos(pa) & \sin(pa) \\ -\sin(pa) & \cos(pa) \end{bmatrix} \quad \text{circular} \begin{bmatrix} e^{-ipa} & 0 \\ 0 & e^{ipa} \end{bmatrix}$$

Parameters

parallactic_angles [`cupy.ndarray`] floating point parallactic angles. Of shape `(pa0, pa1, ..., pan)`.

feed_type [{`'linear'`, `'circular'`}] The type of feed

Returns

feed_matrix [`cupy.ndarray`] Feed rotation matrix of shape $(pa0, pa1, \dots, pan, 2, 2)$

5.1.3 Dask

<code>predict_vis(time_index, antenna1, antenna2)</code>	Multiply Jones terms together to form model visibilities according to the following formula:
<code>phase_delay(lm, uvw, frequency)</code>	Computes the phase delay (K) term:
<code>parallactic_angles(times, antenna_positions, ...)</code>	Computes parallactic angles per timestep for the given reference antenna position and field centre.
<code>feed_rotation(parallactic_angles, feed_type)</code>	Computes the 2x2 feed rotation (L) matrix from the parallactic_angles.
<code>transform_sources(lm, parallactic_angles, ...)</code>	Creates beam sampling coordinates suitable for use in <code>beam_cube_dde()</code> by:
<code>beam_cube_dde(beam, coords, l_grid, m_grid, ...)</code>	Computes Direction Dependent Effects (E) by sampling complex values in beam at the coordinates coords.
<code>zernike_dde(coords, coeffs, noll_index)</code>	Computes Direction Dependent Effects by evaluating Zernicke Polynomials defined by coefficients coeffs and noll indexes noll_index at the specified coordinates coords.

`africanus.rime.dask.predict_vis` (*time_index*, *antenna1*, *antenna2*, *dde1_jones=None*, *source_coh=None*, *dde2_jones=None*, *dde1_jones=None*, *base_vis=None*, *dde2_jones=None*)

Multiply Jones terms together to form model visibilities according to the following formula:

$$V_{pq} = G_p \left(B_{pq} + \sum_s A_{ps} X_{pqs} A_{qs}^H \right) G_q^H$$

where for antenna p and q , and source s :

- B_{pq} represent base coherencies.
- E_{ps} represents Direction-Dependent Jones terms.
- X_{pqs} represents a coherency matrix (per-source).
- G_p represents Direction-Independent Jones terms.

Generally, E_{ps} , G_p , X_{pqs} should be formed by using the [RIME API](#) functions and combining them together with `einsum()`.

Please read the Notes

Parameters

time_index [`dask.array.Array`] Time index used to look up the antenna Jones index for a particular baseline. shape $(row,)$.

antenna1 [`dask.array.Array`] Antenna 1 index used to look up the antenna Jones for a particular baseline. with shape $(row,)$.

antenna2 [`dask.array.Array`] Antenna 2 index used to look up the antenna Jones for a particular baseline. with shape $(row,)$.

dde1_jones [`dask.array.Array`, optional] A_{ps} Direction-Dependent Jones terms for the first antenna. shape $(source, time, ant, chan, corr_1, corr_2)$

source_coh [dask.array.Array, optional] X_{pq} Direction-Dependent Coherency matrix for the baseline. with shape (source, row, chan, corr_1, corr_2)

dde2_jones [dask.array.Array, optional] A_{qs} Direction-Dependent Jones terms for the second antenna. shape (source, time, ant, chan, corr_1, corr_2)

die1_jones [dask.array.Array, optional] G_{ps} Direction-Independent Jones terms for the first antenna of the baseline. with shape (time, ant, chan, corr_1, corr_2)

base_vis [dask.array.Array, optional] B_{pq} base visibilities, added to source coherency summation *before* multiplication with *die1_jones* and *die2_jones*.

die2_jones [dask.array.Array, optional] G_{ps} Direction-Independent Jones terms for the second antenna of the baseline. with shape (time, ant, chan, corr_1, corr_2)

Returns

visibilities [dask.array.Array] Model visibilities of shape (row, chan, corr_1, corr_2)

Notes

- Direction-Dependent terms (dde{1,2}_jones) and Independent (die{1,2}_jones) are optional, but if one is present, the other must be present.
- The inputs to this function involve row, time and ant (antenna) dimensions.
- Each row is associated with a pair of antenna Jones matrices at a particular timestep via the time_index, antennal and antenna2 inputs.
- The row dimension must be an increasing partial order in time.
 - The ant dimension should only contain a single chunk equal to the number of antenna. Since each row can contain any antenna, random access must be preserved along this dimension.
 - The chunks in the row and time dimension **must** align. This subtle point **must be understood otherwise invalid results will be produced** by the chunking scheme. In the example below we have four unique time indices [0, 1, 2, 3], and four unique antenna [0, 1, 2, 3] indexing 10 rows.

```
# Row indices into the time/antenna indexed arrays
time_idx = np.asarray([0,0,1,1,2,2,2,2,3,3])
ant1 = np.asarray([0,0,0,0,1,1,1,2,2,3])
ant2 = np.asarray([0,1,2,3,1,2,3,2,3,3])
```

A reasonable chunking scheme for the row and time dimension would be (4, 4, 2) and (2, 1, 1) respectively. Another way of explaining this is that the first four rows contain two unique timesteps, the second four rows contain one unique timestep and the last two rows contain one unique timestep.

Some rules of thumb:

1. The number chunks in row and time must match although the individual chunk sizes need not.
2. Unique timesteps should not be split across row chunks.
3. For a Measurement Set whose rows are ordered on the TIME column, the following is a good way of obtaining the row chunking strategy:

```
import numpy as np
import pyrap.tables as pt

ms = pt.table("data.ms")
```

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```
times = ms.getcol("TIME")
unique_times, chunks = np.unique(times, return_counts=True)
```

4. Use `aggregate_chunks()` to aggregate multiple row and time chunks into chunks large enough such that functions operating on the resulting data can drop the GIL and spend time processing the data. Expanding the previous example:

```
# Aggregate row
utimes = unique_times.size
# Single chunk for each unique time
time_chunks = (1,)*utimes
# Aggregate row chunks into chunks <= 10000
aggregate_chunks((chunks, time_chunks), (10000, utimes))
```

`africanus.rime.dask.phase_delay(lm, uvw, frequency)`

Computes the phase delay (K) term:

$$e^{-2\pi i(ul+vm+w(n-1))}$$

$$\text{where } n = \sqrt{1 - l^2 - m^2}$$

Parameters

lm [`dask.array.Array`] LM coordinates of shape (source, 2) with L and M components in the last dimension.

uvw [`dask.array.Array`] UVW coordinates of shape (row, 3) with U, V and W components in the last dimension.

frequency [`dask.array.Array`] frequencies of shape (chan,)

Returns

complex_phase [`dask.array.Array`] complex of shape (source, row, chan)

Notes

Corresponds to the complex exponential of the [Van Cittert-Zernike Theorem](#).

[MeqTrees](#) uses a positive sign convention and so any UVW coordinates must be inverted in order for their phase delay terms (and therefore visibilities) to agree.

`africanus.rime.dask.parallactic_angles(times, antenna_positions, field_centre, **kwargs)`

Computes parallactic angles per timestep for the given reference antenna position and field centre.

Parameters

times [`dask.array.Array`] Array of Mean Julian Date times in *seconds* with shape (time,)

antenna_positions [`dask.array.Array`] Antenna positions of shape (ant, 3) in *metres* in the *ITRF* frame.

field_centre [`dask.array.Array`] Field centre of shape (2,) in *radians*

backend [{‘casa’, ‘test’}, optional] Backend to use for calculating the parallactic angles.

- `casa` defers to an implementation depending on `python-casacore`. This backend should be used by default.

- `test` creates parallactic angles by multiplying the `times` and `antenna_position` arrays. It exist solely for testing.

Returns

parallactic_angles [`dask.array.Array`] Parallactic angles of shape `(time, ant)`

`africanus.rime.dask.feed_rotation(parallactic_angles, feed_type)`

Computes the 2x2 feed rotation (L) matrix from the `parallactic_angles`.

$$\text{linear} \begin{bmatrix} \cos(pa) & \sin(pa) \\ -\sin(pa) & \cos(pa) \end{bmatrix} \quad \text{circular} \begin{bmatrix} e^{-ipa} & 0 \\ 0 & e^{ipa} \end{bmatrix}$$

Parameters

parallactic_angles [`numpy.ndarray`] floating point parallactic angles. Of shape `(pa0, pa1, ..., pan)`.

feed_type [{`'linear'`, `'circular'`}] The type of feed

Returns

feed_matrix [`numpy.ndarray`] Feed rotation matrix of shape `(pa0, pa1, ..., pan, 2, 2)`

`africanus.rime.dask.transform_sources(lm, parallactic_angles, pointing_errors, antenna_scaling, frequency, dtype=None)`

Creates beam sampling coordinates suitable for use in `beam_cube_dde()` by:

1. Rotating `lm` coordinates by the `parallactic_angles`
2. Adding `pointing_errors`
3. Scaling by `antenna_scaling`

Parameters

lm [`dask.array.Array`] LM coordinates of shape `(src, 2)` in radians offset from the phase centre.

parallactic_angles [`dask.array.Array`] parallactic angles of shape `(time, antenna)` in radians.

pointing_errors [`dask.array.Array`] LM pointing errors for each antenna at each timestep in radians. Has shape `(time, antenna, 2)`

antenna_scaling [`dask.array.Array`] antenna scaling factor for each channel and each antenna. Has shape `(antenna, chan)`

frequency [`dask.array.Array`] frequencies for each channel. Has shape `(chan,)`

dtype [`numpy.dtype`, optional] Numpy dtype of result array. Should be `float32` or `float64`. Defaults to `float64`

Returns

coords [`dask.array.Array`] coordinates of shape `(3, src, time, antenna, chan)` where each coordinate component represents **l**, **m** and **frequency**, respectively.

`africanus.rime.dask.beam_cube_dde(beam, coords, l_grid, m_grid, freq_grid, spline_order=1, mode='nearest')`

Computes Direction Dependent Effects (E) by sampling complex values in `beam` at the coordinates `coords`.

Both real and imaginary beam values are sampled at the given coordinates and normalised to form a `mean` of `circular` quantities.

`l_grid`, `m_grid` and `freq_grid` can be obtained from `beam_grids()`.

Parameters

beam [`dask.array.Array`] complex beam cube of shape `(beam_lw, beam_mh, beam_nud, corr_1, corr_2)` where `beam_lw` is the grid width of the `l` dimension, `beam_mh` is the grid height of the `m` dimension and `beam_nud` is the grid depth of the frequency dimension. Either `corr_1` or both `corr_1` and `corr_2` may be present, representing 1, 2 or 2x2 correlations respectively.

coords [`dask.array.Array`] beam cube coordinates of shape `(coords, dim_1, ..., dim_n)` where `coord` always has size 3 and refers to `(l,m,frequency)`.

l_grid [`dask.array.Array`] Monotonically *increasing* or *decreasing* grid values for the `l` axis, with shape `(beam_lw,)`. If decreasing, the

m_grid [`dask.array.Array`] Monotonically *increasing* or *decreasing* grid values for the `m` axis, with shape `(beam_mh,)`

freq_grid [`dask.array.Array`] Monotonically increasing grid values for the frequency axis, with shape `(beam_nud,)`

spline_order [int] Spline order to use in `scipy.ndimage.interpolation.map_coordinates()`. Defaults to 1 ('linear')

mode [str] Border mode to use in `scipy.ndimage.interpolation.map_coordinates()` Defaults to 'nearest'

Returns

dde [`dask.array.Array`] Sampled complex beam values at the specified coordinates with shape `(dim_1, ..., dim_n, corr_1, corr_2)`

`africanus.rime.dask.zernike_dde(coords, coeffs, noll_index)`

Computes Direction Dependent Effects by evaluating [Zernicke Polynomials](#) defined by coefficients `coeffs` and noll indexes `noll_index` at the specified coordinates `coords`.

Decomposition of a voxel beam cube into Zernicke polynomial coefficients can be achieved through the use of the [eidos](#) package.

Parameters

coords [`dask.array.Array`] Float coordinates at which to evaluate the zernike polynomials. Has shape `(3, source, time, ant, chan)`. The three components in the first dimension represent `l`, `m` and frequency coordinates, respectively.

coeffs [`dask.array.Array`] complex Zernicke polynomial coefficients. Has shape `(ant, chan, corr_1, ..., corr_n, poly)` where `poly` is the number of polynomial coefficients and `corr_1, ..., corr_n` are a variable number of correlation dimensions.

noll_index [`dask.array.Array`] Noll index associated with each polynomial coefficient. Has shape `(ant, chan, corr_1, ..., corr_n, poly)`.

Returns

dde [`dask.array.Array`] complex values with shape `(source, time, ant, chan, corr_1, ..., corr_n)`

5.2 Direct Fourier Transform

Functions used to compute the discretised direct Fourier transform (DFT) for an ideal unpolarised interferometer. The DFT for an ideal interferometer is defined as

$$V(u, v, w) = \int I(l, m) e^{-2\pi i(ul+vm+w(n-1))} \frac{dl dm}{n}$$

where u, v, w are data (visibility V) space coordinates and l, m, n are signal (image I) space coordinates. We adopt the convention where we absorb the fixed coordinate n in the denominator into the image. Note that the data space coordinates have an implicit dependence on frequency and time and that the image has an implicit dependence on frequency. The discretised form of the DFT can be written as

$$V(u, v, w) = \sum_s e^{-2\pi i(ul_s+vm_s+w(n_s-1))} \cdot I_s$$

where s labels the source (or pixel) location. This can be cast into a matrix equation as follows

$$V = RI$$

where R is the operator that maps an image to visibility space. This mapping is implemented by the `im_to_vis()` function. An imaging algorithm also requires the adjoint denoted R^\dagger which is simply the complex conjugate transpose of R . The dirty image is obtained by applying the adjoint operator to the visibilities

$$I^D = R^\dagger V$$

This is implemented by the `vis_to_im()` function. Note that an imaging algorithm using these operators will actually reconstruct $\frac{I}{n}$ but that it is trivial to obtain I since n is known at each location in the image.

5.2.1 Numpy

<code>im_to_vis(image, uvw, lm, frequency[, dtype])</code>	Computes the discrete image to visibility mapping of an ideal unpolarised interferometer :
<code>vis_to_im(vis, uvw, lm, frequency[, dtype])</code>	Computes visibility to image mapping of an ideal unpolarised interferometer:

`africanus.dft.im_to_vis(image, uvw, lm, frequency, dtype=None)`

Computes the discrete image to visibility mapping of an ideal unpolarised interferometer :

$$\sum_s e^{-2\pi i(ul_s+vm_s+w(n_s-1))} \cdot I_s$$

Parameters

image [`numpy.ndarray`] image of shape `(source, chan)` The Stokes I intensity in each pixel (flatten 2D array per channel).

uvw [`numpy.ndarray`] UVW coordinates of shape `(row, 3)` with U, V and W components in the last dimension.

lm [`numpy.ndarray`] LM coordinates of shape `(source, 2)` with L and M components in the last dimension.

frequency [`numpy.ndarray`] frequencies of shape `(chan,)`

dtype [np.dtype, optional] Datatype of result. Should be either np.complex64 or np.complex128. If None, `numpy.result_type()` is used to infer the data type from the inputs.

Returns

visibilities [numpy.ndarray] complex of shape (row, chan)

`africanus.dft.vis_to_im(vis, uvw, lm, frequency, dtype=None)`

Computes visibility to image mapping of an ideal unpolarised interferometer:

$$\sum_k e^{2\pi i(u_k l + v_k m + w_k(n-1))} \cdot V_k$$

Parameters

vis [numpy.ndarray] visibilities of shape (row, chan) The Stokes I visibilities of which to compute a dirty image

uvw [numpy.ndarray] UVW coordinates of shape (row, 3) with U, V and W components in the last dimension.

lm [numpy.ndarray] LM coordinates of shape (source, 2) with L and M components in the last dimension.

frequency [numpy.ndarray] frequencies of shape (chan,)

dtype [np.dtype, optional] Datatype of result. Should be either np.float32 or np.float64. If None, `numpy.result_type()` is used to infer the data type from the inputs.

Returns

image [numpy.ndarray] float of shape (source, chan)

5.2.2 Dask

<code>im_to_vis(image, uvw, lm, frequency[, dtype])</code>	Computes the discrete image to visibility mapping of an ideal unpolarised interferometer :
<code>vis_to_im(vis, uvw, lm, frequency[, dtype])</code>	Computes visibility to image mapping of an ideal unpolarised interferometer:

`africanus.dft.dask.im_to_vis(image, uvw, lm, frequency, dtype=<type 'numpy.complex128'>)`

Computes the discrete image to visibility mapping of an ideal unpolarised interferometer :

$$\sum_s e^{-2\pi i(ul_s + vm_s + w(n_s-1))} \cdot I_s$$

Parameters

image [dask.array.Array] image of shape (source, chan) The Stokes I intensity in each pixel (flatten 2D array per channel).

uvw [dask.array.Array] UVW coordinates of shape (row, 3) with U, V and W components in the last dimension.

lm [dask.array.Array] LM coordinates of shape (source, 2) with L and M components in the last dimension.

frequency [dask.array.Array] frequencies of shape (chan,)

dtype [np.dtype, optional] Datatype of result. Should be either np.complex64 or np.complex128. If None, `numpy.result_type()` is used to infer the data type from the inputs.

Returns

visibilities [dask.array.Array] complex of shape (row, chan)

`africanus.dft.dask.vis_to_im(vis, uvw, lm, frequency, dtype=<type 'numpy.float64'>)`

Computes visibility to image mapping of an ideal unpolarised interferometer:

$$\sum_k e^{2\pi i(u_k l + v_k m + w_k(n-1))} \cdot V_k$$

Parameters

vis [dask.array.Array] visibilities of shape (row, chan) The Stokes I visibilities of which to compute a dirty image

uvw [dask.array.Array] UVW coordinates of shape (row, 3) with U, V and W components in the last dimension.

lm [dask.array.Array] LM coordinates of shape (source, 2) with L and M components in the last dimension.

frequency [dask.array.Array] frequencies of shape (chan,)

dtype [np.dtype, optional] Datatype of result. Should be either np.float32 or np.float64. If None, `numpy.result_type()` is used to infer the data type from the inputs.

Returns

image [dask.array.Array] float of shape (source, chan)

5.3 Gridding and Degriding

This section contains routines for

1. Gridding complex visibilities onto an image.
2. Degriding complex visibilities from an image.

5.3.1 Simple

Gridding with no correction for the W-term.

Numpy

<code>grid(vis, uvw, flags, weights, ref_wave, ...)</code>	Convolutional gridder which grids visibilities <code>vis</code> at the specified <code>uvw</code> coordinates and <code>ref_wave</code> reference wavelengths using the specified <code>convolution_filter</code> .
<code>degrid(grid, uvw, weights, ref_wave, ...[, ...])</code>	Convolutional degridder (continuum)

`africanus.gridding.simple.grid(vis, uvw, flags, weights, ref_wave, convolution_filter, cell_size, nx=1024, ny=1024, grid=None)`

Convolutional gridder which grids visibilities `vis` at the specified `uvw` coordinates and `ref_wave` reference wavelengths using the specified `convolution_filter`.

Variable numbers of correlations are supported.

- `(row, chan, corr_1, corr_2)` `vis` will result in a `(ny, nx, corr_1, corr_2)` grid.
- `(row, chan, corr_1)` `vis` will result in a `(ny, nx, corr_1)` grid.

Parameters

vis [np.ndarray] complex visibility array of shape `(row, chan, corr_1, corr_2)`

uvw [np.ndarray] float64 array of UVW coordinates of shape `(row, 3)` in wavelengths.

weights [np.ndarray] float32 or float64 array of weights. Set this to `np.ones_like(vis, dtype=np.float32)` as default.

flags [np.ndarray] flagged array of shape `(row, chan, corr_1, corr_2)`. Any positive quantity will indicate that the corresponding visibility should be flagged. Set to `np.zeros_like(vis, dtype=np.bool)` as default.

ref_wave [np.ndarray] float64 array of wavelengths of shape `(chan,)`

convolution_filter [*ConvolutionFilter*] Convolution filter

cell_size [float] Cell size in arcseconds.

nx [integer, optional] Size of the grid's X dimension

ny [integer, optional] Size of the grid's Y dimension

grid [np.ndarray, optional] complex64/complex128 array of shape `(ny, nx, corr_1, corr_2)` If supplied, this array will be used as the gridding target, and `nx` and `ny` will be derived from this grid's dimensions.

Returns

np.ndarray `(ny, nx, corr_1, corr_2)` complex ndarray of gridded visibilities. The number of correlations may vary, depending on the shape of `vis`.

`africanus.gridding.simple.degrid(grid, uvw, weights, ref_wave, convolution_filter, cell_size, dtype=<type 'numpy.complex64'>)`

Convolutional degridding (continuum)

Variable numbers of correlations are supported.

- `(ny, nx, corr_1, corr_2)` grid will result in a `(row, chan, corr_1, corr_2)` `vis`
- `(ny, nx, corr_1)` grid will result in a `(row, chan, corr_1)` `vis`

Parameters

grid [np.ndarray] float or complex grid of visibilities of shape `(ny, nx, corr_1, corr_2)`

uvw [np.ndarray] float64 array of UVW coordinates of shape `(row, 3)` in wavelengths.

weights [np.ndarray] float32 or float64 array of weights. Set this to `np.ones_like(vis, dtype=np.float32)` as default.

ref_wave [np.ndarray] float64 array of wavelengths of shape `(chan,)`

convolution_filter [*ConvolutionFilter*] Convolution Filter

cell_size [float] Cell size in arcseconds.

dtype [`numpy.dtype`] Data type of the visibilities

Returns

np.ndarray (row, chan, corr_1, corr_2) complex ndarray of visibilities

Dask

<code>grid(vis, uvw, flags, weights, ref_wave, ...)</code>	Convolutional gridder which grids visibilities <code>vis</code> at the specified <code>uvw</code> coordinates and <code>ref_wave</code> reference wavelengths using the specified <code>convolution_filter</code> .
<code>degrid(grid, uvw, weights, ref_wave, ...)</code>	Convolutional degridding (continuum)

`africanus.gridding.simple.dask.grid(vis, uvw, flags, weights, ref_wave, convolution_filter, cell_size, nx=1024, ny=1024)`

Convolutional gridder which grids visibilities `vis` at the specified `uvw` coordinates and `ref_wave` reference wavelengths using the specified `convolution_filter`.

Variable numbers of correlations are supported.

- (row, chan, corr_1, corr_2) `vis` will result in a (ny, nx, corr_1, corr_2) grid.
- (row, chan, corr_1) `vis` will result in a (ny, nx, corr_1) grid.

Parameters

vis [np.ndarray] complex visibility array of shape (row, chan, corr_1, corr_2)

uvw [np.ndarray] float64 array of UVW coordinates of shape (row, 3) in wavelengths.

weights [np.ndarray] float32 or float64 array of weights. Set this to `da.ones_like(vis, dtype=np.float32)` as default.

flags [np.ndarray] flagged array of shape (row, chan, corr_1, corr_2). Any positive quantity will indicate that the corresponding visibility should be flagged. Set to `da.zeros_like(vis, dtype=np.bool)` as default.

ref_wave [np.ndarray] float64 array of wavelengths of shape (chan,)

convolution_filter [`ConvolutionFilter`] Convolution filter

cell_size [float] Cell size in arcseconds.

nx [integer, optional] Size of the grid's X dimension

ny [integer, optional] Size of the grid's Y dimension

grid [np.ndarray, optional] complex64/complex128 array of shape (ny, nx, corr_1, corr_2) If supplied, this array will be used as the gridding target, and `nx` and `ny` will be derived from this grid's dimensions.

Returns

np.ndarray (ny, nx, corr_1, corr_2) complex ndarray of gridded visibilities. The number of correlations may vary, depending on the shape of `vis`.

`africanus.gridding.simple.dask.degrid`(*grid*, *uvw*, *weights*, *ref_wave*, *convolution_filter*, *cell_size*)

Convolutional degridding (continuum)

Variable numbers of correlations are supported.

- (ny, nx, corr_1, corr_2) grid will result in a (row, chan, corr_1, corr_2) vis
- (ny, nx, corr_1) grid will result in a (row, chan, corr_1) vis

Parameters

grid [np.ndarray] float or complex grid of visibilities of shape (ny, nx, corr_1, corr_2)

uvw [np.ndarray] float64 array of UVW coordinates of shape (row, 3) in wavelengths.

weights [np.ndarray] float32 or float64 array of weights. Set this to `da.ones_like(vis, dtype=np.float32)` as default.

ref_wave [np.ndarray] float64 array of wavelengths of shape (chan,)

convolution_filter [*ConvolutionFilter*] Convolution Filter

cell_size [float] Cell size in arcseconds.

dtype [numpy.dtype] Data type of the visibilities

Returns

np.ndarray (row, chan, corr_1, corr_2) complex ndarray of visibilities

5.3.2 W Stacking

This is currently experimental

Implements W-Stacking as described in [WSClean](#).

<code>w_stacking_layers</code> (w_min, w_max, l, m)	Computes the number of w-layers given the minimum and maximum W coordinates, as well as the l and m coordinates.
<code>w_stacking_bins</code> (w_min, w_max, w_layers)	Returns the W coordinate bins appropriate for the observation parameters, given the minimum and maximum W coordinates and the number of W layers.
<code>w_stacking_centroids</code> (w_bins)	Returns the W coordinate centroids for each W layer.
<code>grid</code> (vis, uvw, flags, weights, ref_wave, ...)	Convolutional W-stacking gridded.
<code>degrid</code> (grids, uvw, weights, ref_wave, ..., ..., ...)	Convolutional W-stacking degridding (continuum)

`africanus.gridding.wstack.w_stacking_layers` (*w_min*, *w_max*, *l*, *m*)

Computes the number of w-layers given the minimum and maximum W coordinates, as well as the l and m coordinates.

$$N_{wlay} \gg 2\pi (w_{max} - w_{min}) \max_{l,m} \left(1 - \sqrt{1 - l^2 - m^2} \right)$$

Parameters

w_min [float] Minimum W coordinate in wavelengths.

w_max [float] Maximum W coordinate in wavelengths.

l [numpy.ndarray] l coordinates

m [numpy.ndarray] m coordinates

Returns

int Number of w-layers

`africanus.gridding.wstack.w_stacking_bins(w_min, w_max, w_layers)`

Returns the W coordinate bins appropriate for the observation parameters, given the minimum and maximum W coordinates and the number of W layers.

W coordinates can be binned by calling

```
w_bins = np.digitize(w, bins) - 1
```

Parameters

w_min [float] Minimum W coordinate in wavelengths.

w_max [float] Maximum W coordinate in wavelengths.

w_layers [int] Number of w layers

Returns

:class:'numpy.ndarray' W-coordinate bins of shape `(nw + 1,)`.

Notes

A small epsilon is added to `w_max` to force this W coordinate into the last bin.

`africanus.gridding.wstack.w_stacking_centroids(w_bins)`

Returns the W coordinate centroids for each W layer. Computed from bins produced by `w_stacking_bins()`.

Parameters

w_bins [numpy.ndarray] W stacking bins of shape `(nw + 1,)`

Returns

:class:'numpy.ndarray' W-coordinate centroids of shape `(nw,)` in wavelengths.

`africanus.gridding.wstack.grid(vis, uvw, flags, weights, ref_wave, convolution_filter, w_bins, cell_size, nx=1024, ny=1024, grids=None)`

Convolutional W-stacking gridder.

This function grids visibilities `vis` onto multiple grids, each associated with a W-layer defined by `w_bins`. The W coordinate of the `uvw` array is used to bin the visibility into the appropriate grid.

Variable numbers of correlations are supported.

- `(row, chan, corr_1, corr_2)` `vis` will result in a `(ny, nx, corr_1, corr_2)` grid.
- `(row, chan, corr_1)` `vis` will result in a `(ny, nx, corr_1)` grid.

Parameters

vis [numpy.ndarray] complex visibility array of shape `(row, chan, corr_1, corr_2)`

uvw [numpy.ndarray] float64 array of UVW coordinates of shape `(row, 3)`

weights [numpy.ndarray] float32 or float64 array of weights. Set this to `np.ones_like(vis, dtype=np.float32)` as default.

flags [np.ndarray] flagged array of shape (row, chan, corr_1, corr_2). Any positive quantity will indicate that the corresponding visibility should be flagged. Set to np.zeros_like(vis, dtype=np.bool) as default.

ref_wave [np.ndarray] float64 array of wavelengths of shape (chan,)

convolution_filter [*ConvolutionFilter*] Convolution filter

w_bins [numpy.ndarray] W coordinate bins of shape (nw + 1,)

cell_size [float] Cell size in arcseconds.

nx [integer, optional] Size of the grid's X dimension

ny [integer, optional] Size of the grid's Y dimension

grids [list of np.ndarray, optional] list of complex arrays of length nw, each with shape (ny, nx, corr_1, corr_2). If supplied, this array will be used as the gridding target, and nx and ny will be derived from the grid's dimensions.

Returns

list of np.ndarray list of complex arrays of gridded visibilities, of length nw, each with shape (ny, nx, corr_1, corr_2). The number of correlations may vary, depending on the shape of vis.

africanus.gridding.wstack.**degrid**(grids, uvw, weights, ref_wave, convolution_filter, w_bins, cell_size, dtype=<type 'numpy.complex64'>)

Convolutional W-stacking degridding (continuum)

Variable numbers of correlations are supported.

- (ny, nx, corr_1, corr_2) grid will result in a (row, chan, corr_1, corr_2) vis
- (ny, nx, corr_1) grid will result in a (row, chan, corr_1) vis

Parameters

grids [list of np.ndarray] list of visibility grids of length nw. of shape (ny, nx, corr_1, corr_2)

uvw [np.ndarray] float64 array of UVW coordinates of shape (row, 3)

weights [np.ndarray] float32 or float64 array of weights. Set this to np.ones_like(vis, dtype=np.float32) as default.

ref_wave [np.ndarray] float64 array of wavelengths of shape (chan,)

convolution_filter [*ConvolutionFilter*] Convolution Filter

w_bins [numpy.ndarray] W coordinate bins of shape (nw + 1,)

cell_size [float] Cell size in arcseconds.

dtype [numpy.dtype, optional] Numpy type of the resulting array. Defaults to numpy.complex64.

Returns

np.ndarray (row, chan, corr_1, corr_2) complex ndarray of visibilities

5.3.3 Utilities

<code>estimate_cell_size(u, v, wavelength[, ...])</code>	Estimate the cell size in arcseconds given baseline <code>u</code> and <code>v</code> coordinates, as well as the wavelengths, λ .
--	--

`africanus.gridding.util.estimate_cell_size(u, v, wavelength, factor=3.0, ny=None, nx=None)`

Estimate the cell size in arcseconds given baseline `u` and `v` coordinates, as well as the wavelengths, λ .

The cell size is computed as:

$$\Delta u = 1.0 / (2 \times \text{factor} \times \max(|u|) / \min(\lambda))$$

$$\Delta v = 1.0 / (2 \times \text{factor} \times \max(|v|) / \min(\lambda))$$

If `ny` and `nx` are provided the following checks are performed and exceptions are raised on failure:

$$\Delta u * \text{ny} \leq \min(\lambda) / \min(|u|)$$

$$\Delta v * \text{nx} \leq \min(\lambda) / \min(|v|)$$

Parameters

u [`numpy.ndarray` or float] Maximum `u` coordinate in metres.

v [`numpy.ndarray` or float] Maximum `v` coordinate in metres.

wavelength [`numpy.ndarray` or float] Wavelengths, in metres.

factor [float, optional] Scaling factor

ny [int, optional] Grid `y` dimension

nx [int, optional] Grid `x` dimension

Returns

:class:‘`numpy.ndarray`’ Cell size of `u` and `v` in arcseconds with shape `(2,)`

Raises

ValueError If the cell size criteria are not matched.

5.4 Convolution Filters

Convolution filters suitable for use in gridding and degriding.

5.4.1 API

<code>convolution_filter(half_support, ...)</code>	Create a 2D Convolution Filter suitable for use with gridding and degriding functions.
--	--

`africanus.filters.convolution_filter(half_support, oversampling_factor, filter_type, **kwargs)`

Create a 2D Convolution Filter suitable for use with gridding and degriding functions.

Parameters

half_support [integer] Half support (`N`) of the filter. The filter has a full support of `N*2 + 3` taps. Two of the taps exist as padding.

oversampling_factor [integer] Number of spaces in-between grid-steps (improves gridding/degridding accuracy)

filter_type [{ 'kaiser-bessel', 'sinc' }] Filter type. See [Convolution Filters](#) for further information.

beta [float, optional] Beta shape parameter for [Kaiser Bessel](#) filters.

normalise [{ True, False }] Normalise the filter by the it's volume. Defaults to `True`.

Returns

:class:'ConvolutionFilter' namedtuple containing filter attributes

```
africanus.filters.ConvolutionFilter = <class 'africanus.filters.conv_filters.ConvolutionFi
```

5.4.2 Kaiser Bessel

The [Kaiser Bessel](#) function.

<code>kaiser_bessel(u, W, beta)</code>	Compute a 1D Kaiser Bessel filter as defined in Selection of a Convolution Function for Fourier Inversion Using Gridding .
<code>kaiser_bessel_with_sinc(u, W, oversample, beta)</code>	Produces a filter composed of Kaiser Bessel multiplied by a sinc.
<code>kaiser_bessel_fourier(x, W, beta)</code>	Computes the Fourier Transform of a 1D Kaiser Bessel filter.
<code>estimate_kaiser_bessel_beta(W)</code>	Estimate the kaiser bessel beta using the following heuristic:

```
africanus.filters.kaiser_bessel_filter.kaiser_bessel(u, W, beta)
```

Compute a 1D Kaiser Bessel filter as defined in [Selection of a Convolution Function for Fourier Inversion Using Gridding](#).

Parameters

u [numpy.ndarray] Filter positions

W [int] Width of the filter

beta [float, optional] Kaiser Bessel shape parameter

Returns

:class:'numpy.ndarray' Kaiser Bessel filter with the same shape as *u*

```
africanus.filters.kaiser_bessel_filter.kaiser_bessel_with_sinc(u, W, oversample, beta, normalise=True)
```

Produces a filter composed of Kaiser Bessel multiplied by a sinc.

Accounts for the oversampling factor, as well as normalising the filter.

Parameters

u [numpy.ndarray] Filter positions

W [int] Width of the filter

oversample [int] Oversampling factor

beta [float] Kaiser Bessel shape parameter

normalise [optional, {True, False}] True if the filter should be normalised

Returns

:class:'numpy.ndarray' Filter with the same shape as *u*

`africanus.filters.kaiser_bessel_filter.kaiser_bessel_fourier(x, W, beta)`

Computes the Fourier Transform of a 1D Kaiser Bessel filter. as defined in [Selection of a Convolution Function for Fourier Inversion Using Gridding](#).

Parameters

x [`numpy.ndarray`] Filter positions

W [int] Width of the filter.

beta [float] Kaiser bessel shape parameter

Returns

:class:'numpy.ndarray' Fourier Transform of the Kaiser Bessel, with the same shape as *x*.

`africanus.filters.kaiser_bessel_filter.estimate_kaiser_bessel_beta(W)`

Estimate the kaiser bessel beta using the following heuristic:

$$\beta = 2.34 \times W$$

Derived from [Nonuniform fast Fourier transforms using min-max interpolation](#).

Parameters

W [int] Width of the filter

Returns

float Kaiser Bessel beta shape parameter

5.4.3 Sinc

The [Sinc](#) function.

5.5 Deconvolution Algorithms

5.6 Coordinate Transforms

5.6.1 Numpy

<code>radec_to_lm(radec[, phase_centre])</code>	Converts Right-Ascension/Declination coordinates in radians to a Direction Cosine lm coordinates, relative to the Phase Centre.
<code>radec_to_lmn(radec[, phase_centre])</code>	Converts Right-Ascension/Declination coordinates in radians to a Direction Cosine lm coordinates, relative to the Phase Centre.
<code>lm_to_radec(lm[, phase_centre])</code>	Convert Direction Cosine lm coordinates to Right Ascension/Declination coordinates in radians, relative to the Phase Centre.

Continued on next page

Table 12 – continued from previous page

<code>lmn_to_radec(lmn[, phase_centre])</code>	Convert Direction Cosine lm coordinates to Right Ascension/Declination coordinates in radians, relative to the Phase Centre.
--	--

`africanus.coordinates.radec_to_lm(radec, phase_centre=None)`

Converts Right-Ascension/Declination coordinates in radians to a Direction Cosine lm coordinates, relative to the Phase Centre.

$$l = \cos \delta \sin \Delta\alpha \quad (5.1)$$

$$m = \sin \delta \cos \delta 0 - \cos \delta \sin \delta 0 \cos \Delta\alpha \quad (5.2)$$

$$n = \sqrt{1 - l^2 - m^2} - 1 \quad (5.3)$$

where $\Delta\alpha = \alpha - \alpha 0$ is the difference between the Right Ascension of each coordinate and the phase centre and $\delta 0$ is the Declination of the phase centre.

Parameters

radec [`numpy.ndarray`] radec coordinates of shape `(coord, 2)` where Right-Ascension and Declination are in the last 2 components, respectively.

phase_centre [`numpy.ndarray`, optional] radec coordinates of the Phase Centre. Shape `(2,)`

Returns

:class:'numpy.ndarray' lm Direction Cosines of shape `(coord, 2)`

`africanus.coordinates.radec_to_lmn(radec, phase_centre=None)`

Converts Right-Ascension/Declination coordinates in radians to a Direction Cosine lm coordinates, relative to the Phase Centre.

$$l = \cos \delta \sin \Delta\alpha \quad (5.4)$$

$$m = \sin \delta \cos \delta 0 - \cos \delta \sin \delta 0 \cos \Delta\alpha \quad (5.5)$$

$$n = \sqrt{1 - l^2 - m^2} - 1 \quad (5.6)$$

where $\Delta\alpha = \alpha - \alpha 0$ is the difference between the Right Ascension of each coordinate and the phase centre and $\delta 0$ is the Declination of the phase centre.

Parameters

radec [`numpy.ndarray`] radec coordinates of shape `(coord, 2)` where Right-Ascension and Declination are in the last 2 components, respectively.

phase_centre [`numpy.ndarray`, optional] radec coordinates of the Phase Centre. Shape `(2,)`

Returns

:class:'numpy.ndarray' lm Direction Cosines of shape `(coord, 3)`

`africanus.coordinates.lm_to_radec(lm, phase_centre=None)`

Convert Direction Cosine lm coordinates to Right Ascension/Declination coordinates in radians, relative to the Phase Centre.

$$\delta = \arcsin(m \cos \delta 0 + n \sin \delta 0) \quad (5.7)$$

$$\alpha = \arctan\left(\frac{l}{n \cos \delta 0 - m \sin \delta 0}\right) \quad (5.8)$$

$$(5.9)$$

where α is the Right Ascension of each coordinate and the phase centre and δ_0 is the Declination of the phase centre.

Parameters

lm [`numpy.ndarray`] lm Direction Cosines of shape `(coord, 2)`

phase_centre [`numpy.ndarray`, optional] radec coordinates of the Phase Centre. Shape `(2,)`

Returns

:class:'`numpy.ndarray`' radec coordinates of shape `(coord, 2)` where Right-Ascension and Declination are in the last 2 components, respectively.

`africanus.coordinates.lmn_to_radec(lmn, phase_centre=None)`

Convert Direction Cosine lm coordinates to Right Ascension/Declination coordinates in radians, relative to the Phase Centre.

$$\delta = \arcsin(m \cos \delta_0 + n \sin \delta_0) \quad (5.10)$$

$$\alpha = \arctan\left(\frac{l}{n \cos \delta_0 - m \sin \delta_0}\right) \quad (5.11)$$

$$(5.12)$$

where α is the Right Ascension of each coordinate and the phase centre and δ_0 is the Declination of the phase centre.

Parameters

lmn [`numpy.ndarray`] lm Direction Cosines of shape `(coord, 3)`

phase_centre [`numpy.ndarray`, optional] radec coordinates of the Phase Centre. Shape `(2,)`

Returns

:class:'`numpy.ndarray`' radec coordinates of shape `(coord, 2)` where Right-Ascension and Declination are in the last 2 components, respectively.

5.6.2 Dask

<code>radec_to_lm(radec[, phase_centre])</code>	Converts Right-Ascension/Declination coordinates in radians to a Direction Cosine lm coordinates, relative to the Phase Centre.
<code>radec_to_lmn(radec[, phase_centre])</code>	Converts Right-Ascension/Declination coordinates in radians to a Direction Cosine lm coordinates, relative to the Phase Centre.
<code>lm_to_radec(lm[, phase_centre])</code>	Convert Direction Cosine lm coordinates to Right Ascension/Declination coordinates in radians, relative to the Phase Centre.
<code>lmn_to_radec(lmn[, phase_centre])</code>	Convert Direction Cosine lm coordinates to Right Ascension/Declination coordinates in radians, relative to the Phase Centre.

`africanus.coordinates.dask.radec_to_lm(radec, phase_centre=None)`

Converts Right-Ascension/Declination coordinates in radians to a Direction Cosine lm coordinates, relative to

the Phase Centre.

$$l = \cos \delta \sin \Delta\alpha \quad (5.13)$$

$$m = \sin \delta \cos \delta_0 - \cos \delta \sin \delta_0 \cos \Delta\alpha \quad (5.14)$$

$$n = \sqrt{1 - l^2 - m^2} - 1 \quad (5.15)$$

where $\Delta\alpha = \alpha - \alpha_0$ is the difference between the Right Ascension of each coordinate and the phase centre and δ_0 is the Declination of the phase centre.

Parameters

radec [`dask.array.Array`] radec coordinates of shape `(coord, 2)` where Right-Ascension and Declination are in the last 2 components, respectively.

phase_centre [`dask.array.Array`, optional] radec coordinates of the Phase Centre. Shape `(2,)`

Returns

:class:'dask.array.Array' lm Direction Cosines of shape `(coord, 2)`

`africanus.coordinates.dask.radec_to_lmn(radec, phase_centre=None)`

Converts Right-Ascension/Declination coordinates in radians to a Direction Cosine lm coordinates, relative to the Phase Centre.

$$l = \cos \delta \sin \Delta\alpha \quad (5.16)$$

$$m = \sin \delta \cos \delta_0 - \cos \delta \sin \delta_0 \cos \Delta\alpha \quad (5.17)$$

$$n = \sqrt{1 - l^2 - m^2} - 1 \quad (5.18)$$

where $\Delta\alpha = \alpha - \alpha_0$ is the difference between the Right Ascension of each coordinate and the phase centre and δ_0 is the Declination of the phase centre.

Parameters

radec [`dask.array.Array`] radec coordinates of shape `(coord, 2)` where Right-Ascension and Declination are in the last 2 components, respectively.

phase_centre [`dask.array.Array`, optional] radec coordinates of the Phase Centre. Shape `(2,)`

Returns

:class:'dask.array.Array' lm Direction Cosines of shape `(coord, 3)`

`africanus.coordinates.dask.lm_to_radec(lm, phase_centre=None)`

Convert Direction Cosine lm coordinates to Right Ascension/Declination coordinates in radians, relative to the Phase Centre.

$$\delta = \arcsin(m \cos \delta_0 + n \sin \delta_0) \quad (5.19)$$

$$\alpha = \arctan\left(\frac{l}{n \cos \delta_0 - m \sin \delta_0}\right) \quad (5.20)$$

$$(5.21)$$

where α is the Right Ascension of each coordinate and the phase centre and δ_0 is the Declination of the phase centre.

Parameters

lm [`dask.array.Array`] lm Direction Cosines of shape `(coord, 2)`

phase_centre [`dask.array.Array`, optional] radec coordinates of the Phase Centre. Shape `(2,)`

Returns

:class:‘`dask.array.Array`’ radec coordinates of shape `(coord, 2)` where Right-Ascension and Declination are in the last 2 components, respectively.

`africanus.coordinates.dask.lmn_to_radec(lmn, phase_centre=None)`

Convert Direction Cosine lm coordinates to Right Ascension/Declination coordinates in radians, relative to the Phase Centre.

$$\delta = \arcsin(m \cos \delta_0 + n \sin \delta_0) \quad (5.22)$$

$$\alpha = \arctan\left(\frac{l}{n \cos \delta_0 - m \sin \delta_0}\right) \quad (5.23)$$

$$(5.24)$$

where α is the Right Ascension of each coordinate and the phase centre and δ_0 is the Declination of the phase centre.

Parameters

`lmn` [`dask.array.Array`] lm Direction Cosines of shape `(coord, 3)`

`phase_centre` [`dask.array.Array`, optional] radec coordinates of the Phase Centre. Shape `(2,)`

Returns

:class:‘`dask.array.Array`’ radec coordinates of shape `(coord, 2)` where Right-Ascension and Declination are in the last 2 components, respectively.

5.7 Sky Model

Functionality related to the Sky Model.

5.7.1 Coherency Conversion

Utilities for converting back and forth between stokes parameters and correlations

Numpy

<code>convert(input, input_schema, output_schema)</code>	This function converts forward and backward from stokes I, Q, U, V to both linear XX, XY, YX, YY and circular RR, RL, LR, LL correlations.
--	--

`africanus.model.coherency.convert(input, input_schema, output_schema)`

This function converts forward and backward from stokes I, Q, U, V to both linear XX, XY, YX, YY and circular RR, RL, LR, LL correlations.

For example, we can convert from stokes parameters to linear correlations:

```
stokes.shape == (10, 4, 4)
corrs = convert(stokes, ["I", "Q", "U", "V"],
                 [['XX', 'XY'], ['YX', 'YY']])

assert corrs.shape == (10, 4, 2, 2)
```

Or circular correlations to stokes:

```
vis.shape == (10, 4, 2, 2)

stokes = convert(vis, [['RR', 'RL'], ['LR', 'LL']],
                  ['I', 'Q', 'U', 'V'])

assert stokes.shape == (10, 4, 4)
```

input can output can be arbitrarily nested or ordered lists, but the appropriate inputs must be present to produce the requested outputs.

The elements of input and output may be strings or integers representing stokes parameters or correlations. See the Notes for a full list.

Parameters

input [`numpy.ndarray`] Complex or floating point input data of shape (dim_1, ..., dim_n, icorr_1, ..., icorr_m)

input_schema [list of str or int] A schema describing the icorr_1, ..., icorr_m dimension of input. Must have the same shape as the last dimensions of input.

output_schema [list of str or int] A schema describing the ocorr_1, ..., ocorr_n dimension of the return value.

Returns

result [`numpy.ndarray`] Result of shape (dim_1, ..., dim_n, ocorr_1, ..., ocorr_m) The type may be floating point or promoted to complex depending on the combinations in output.

Notes

Only stokes parameters, linear and circular correlations are currently handled, but the full list of id's and strings as defined in the [CASA documentation](#) is:

```
{ { Undefined: 0, I: 1, Q: 2, U: 3, V: 4, RR: 5, RL: 6, LR: 7, LL: 8,
  XX: 9, XY: 10, YX: 11, YY: 12, RX: 13, RY: 14, LX: 15, LY: 16,
  XR: 17, XL: 18, YR: 19, YL: 20, PP: 21, PQ: 22, QP: 23, QQ:
  24, RCircular: 25, LCircular: 26, Linear: 27, Ptotal: 28,
  Plinear: 29, Pftotal: 30, Pflinear: 31, Pangle: 32 } }
```

Cuda

<code>convert</code> (inputs, input_schema, output_schema)	This function converts forward and backward from stokes I, Q, U, V to both linear XX, XY, YX, YY and circular RR, RL, LR, LL correlations.
--	--

`africanus.model.coherency.cuda.convert` (inputs, input_schema, output_schema)

This function converts forward and backward from stokes I, Q, U, V to both linear XX, XY, YX, YY and circular RR, RL, LR, LL correlations.

For example, we can convert from stokes parameters to linear correlations:


```

stokes.shape == (10, 4, 4)
corrs = convert(stokes, ["I", "Q", "U", "V"],
                  [['XX', 'XY'], ['YX', 'YY']])

assert corrs.shape == (10, 4, 2, 2)

```

Or circular correlations to stokes:

```

vis.shape == (10, 4, 2, 2)

stokes = convert(vis, [['RR', 'RL'], ['LR', 'LL']],
                  ['I', 'Q', 'U', 'V'])

assert stokes.shape == (10, 4, 4)

```

input can output can be arbitrarily nested or ordered lists, but the appropriate inputs must be present to produce the requested outputs.

The elements of input and output may be strings or integers representing stokes parameters or correlations. See the Notes for a full list.

Parameters

- input** [`cupy.ndarray`] Complex or floating point input data of shape (dim_1, ..., dim_n, icorr_1, ..., icorr_m)
- input_schema** [list of str or int] A schema describing the icorr_1, ..., icorr_m dimension of input. Must have the same shape as the last dimensions of input.
- output_schema** [list of str or int] A schema describing the ocorr_1, ..., ocorr_n dimension of the return value.

Returns

- result** [`cupy.ndarray`] Result of shape (dim_1, ..., dim_n, ocorr_1, ..., ocorr_m) The type may be floating point or promoted to complex depending on the combinations in output.

Notes

Only stokes parameters, linear and circular correlations are currently handled, but the full list of id's and strings as defined in the [CASA documentation](#) is:

```

{{ Undefined: 0, I: 1, Q: 2, U: 3, V: 4, RR: 5, RL: 6, LR: 7, LL: 8,
  XX: 9, XY: 10, YX: 11, YY: 12, RX: 13, RY: 14, LX: 15, LY: 16,
  XR: 17, XL: 18, YR: 19, YL: 20, PP: 21, PQ: 22, QP: 23, QQ:
  24, RCircular: 25, LCircular: 26, Linear: 27, Ptotal: 28,
  Plinear: 29, Pftotal: 30, Pflinear: 31, Pangle: 32 }}

```

Dask

`convert`(input, input_schema, output_schema)

This function converts forward and backward from stokes I, Q, U, V to both linear XX, XY, YX, YY and circular RR, RL, LR, LL correlations.

`africanus.model.coherency.dask.convert` (*input*, *input_schema*, *output_schema*)

This function converts forward and backward from stokes I, Q, U, V to both linear XX, XY, YX, YY and circular RR, RL, LR, LL correlations.

For example, we can convert from stokes parameters to linear correlations:

```
stokes.shape == (10, 4, 4)
corrs = convert(stokes, ["I", "Q", "U", "V"],
                  [['XX', 'XY'], ['YX', 'YY']])
assert corrs.shape == (10, 4, 2, 2)
```

Or circular correlations to stokes:

```
vis.shape == (10, 4, 2, 2)
stokes = convert(vis, [['RR', 'RL'], ['LR', 'LL']],
                  ['I', 'Q', 'U', 'V'])
assert stokes.shape == (10, 4, 4)
```

input can output can be arbitrarily nested or ordered lists, but the appropriate inputs must be present to produce the requested outputs.

The elements of *input* and *output* may be strings or integers representing stokes parameters or correlations. See the Notes for a full list.

Parameters

- input** [`dask.array.Array`] Complex or floating point input data of shape (`dim_1`, ..., `dim_n`, `icorr_1`, ..., `icorr_m`)
- input_schema** [list of str or int] A schema describing the `icorr_1`, ..., `icorr_m` dimension of *input*. Must have the same shape as the last dimensions of *input*.
- output_schema** [list of str or int] A schema describing the `ocorr_1`, ..., `ocorr_n` dimension of the return value.

Returns

- result** [`dask.array.Array`] Result of shape (`dim_1`, ..., `dim_n`, `ocorr_1`, ..., `ocorr_m`) The type may be floating point or promoted to complex depending on the combinations in *output*.

Notes

Only stokes parameters, linear and circular correlations are currently handled, but the full list of id's and strings as defined in the [CASA documentation](#) is:

```
{ { Undefined: 0, I: 1, Q: 2, U: 3, V: 4, RR: 5, RL: 6, LR: 7, LL: 8,
  XX: 9, XY: 10, YX: 11, YY: 12, RX: 13, RY: 14, LX: 15, LY: 16,
  XR: 17, XL: 18, YR: 19, YL: 20, PP: 21, PQ: 22, QP: 23, QQ:
  24, RCircular: 25, LCircular: 26, Linear: 27, Ptotal: 28,
  Plinear: 29, Pftotal: 30, Pflinear: 31, Pangle: 32 } }
```

5.7.2 Spectral Model

Functionality for computing a Spectral Model.

Numpy

<code>spectral_model(stokes, spi, ref_freq, frequency)</code>	Compute a spectral model, per polarisation.
---	---

`africanus.model.spectral.spectral_model(stokes, spi, ref_freq, frequency, base=0)`

Compute a spectral model, per polarisation.

$$I(\lambda) = \sum_{i=0} \alpha_i (\lambda/\lambda_0 - 1)^i \text{ where } \alpha_0 = I(\lambda_0) \quad (5.25)$$

$$\ln(I(\lambda)) = \sum_{i=0} \alpha_i \ln(\lambda/\lambda_0)^i \text{ where } \alpha_0 = \ln I_0 \quad (5.26)$$

$$\log_{10}(I(\lambda)) = \sum_{i=0} \alpha_i \log_{10}(\lambda/\lambda_0)^i \text{ where } \alpha_0 = \log_{10} I_0 \quad (5.27)$$

$$(5.28)$$

Parameters

stokes [`numpy.ndarray`] Stokes parameters of shape `(source,)` or `(source, pol)`.
If a `pol` dimension is present, then it must also be present on `spi`.

spi [`numpy.ndarray`] Spectral index of shape `(source, spi-comps)` or `(source, spi-comps, pol)`.

ref_freq [`numpy.ndarray`] Reference frequencies of shape `(source,)`

frequencies [`numpy.ndarray`] Frequencies of shape `(chan,)`

base [{`"std"`, `"log"`, `"log10"`} or {0, 1, 2} or list.] string or corresponding enumeration specifying the polynomial base. Defaults to 0.

If a list is provided, a polynomial base can be specified for each stokes parameter or polarisation in the `pol` dimension.

string specification of the base is only supported in python 3. while the corresponding integer enumerations are supported on all python versions.

Returns

spectral_model [`numpy.ndarray`] Spectral Model of shape `(source, chan)` or `(source, chan, pol)`.

Dask

<code>spectral_model(stokes, spi, ref_freq, ..., [...])</code>	Compute a spectral model, per polarisation.
--	---

`africanus.model.spectral.dask.spectral_model(stokes, spi, ref_freq, frequencies, base=0)`

Compute a spectral model, per polarisation.

$$I(\lambda) = \sum_{i=0} \alpha_i (\lambda/\lambda_0 - 1)^i \text{ where } \alpha_0 = I(\lambda_0) \quad (5.29)$$

$$\ln(I(\lambda)) = \sum_{i=0} \alpha_i \ln(\lambda/\lambda_0)^i \text{ where } \alpha_0 = \ln I_0 \quad (5.30)$$

$$\log_{10}(I(\lambda)) = \sum_{i=0} \alpha_i \log_{10}(\lambda/\lambda_0)^i \text{ where } \alpha_0 = \log_{10} I_0 \quad (5.31)$$

$$(5.32)$$

Parameters

- stokes** [`dask.array.Array`] Stokes parameters of shape `(source,)` or `(source, pol)`. If a `pol` dimension is present, then it must also be present on `spi`.
- spi** [`dask.array.Array`] Spectral index of shape `(source, spi-comps)` or `(source, spi-comps, pol)`.
- ref_freq** [`dask.array.Array`] Reference frequencies of shape `(source,)`
- frequencies** [`dask.array.Array`] Frequencies of shape `(chan,)`
- base** [{`"std"`, `"log"`, `"log10"`} or {0, 1, 2} or list.] string or corresponding enumeration specifying the polynomial base. Defaults to 0.
- If a list is provided, a polynomial base can be specified for each stokes parameter or polarisation in the `pol` dimension.
- string specification of the base is only supported in python 3. while the corresponding integer enumerations are supported on all python versions.

Returns

- spectral_model** [`dask.array.Array`] Spectral Model of shape `(source, chan)` or `(source, chan, pol)`.

5.7.3 Spectral Index

Functionality related to the spectral index.

For example, we may want to compute the spectral indices of components in a sky model defined by

$$I(\nu) = I(\nu_0) \left(\frac{\nu}{\nu_0} \right)^\alpha$$

where ν are frequencies at which we want to construct the intensity of a Stokes I image and the ν_0 is the corresponding reference frequency. The spectral index α determines how quickly the intensity grows or decays as a function of frequency. Given a list of model image components (preferably with the residuals added back in) we can recover the corresponding spectral indices and reference intensities using the `fit_spi_components()` function. This will also return a lower bound on the associated uncertainties on these components.

Numpy

<code>fit_spi_components(data, weights, freqs, freq0)</code>	Computes the spectral indices and the intensity at the reference frequency of a spectral index model:
--	---

```
africanus.model.spi.fit_spi_components(data, weights, freqs, freq0,
                                       l0i=None, tol=1e-06, maxiter=100, dtype=<type
                                       'numpy.float64'>)
```

Computes the spectral indices and the intensity at the reference frequency of a spectral index model:

$$I(\nu) = I(\nu_0) \left(\frac{\nu}{\nu_0} \right)^\alpha$$

Parameters

- data** [`numpy.ndarray`] array of shape `(comps, chan)` The noisy data as a function of frequency.

weights [`numpy.ndarray`] array of shape `(chan,)` Inverse of variance on each frequency axis.

freqs [`numpy.ndarray`] frequencies of shape `(chan,)`

freq0 [float] Reference frequency

alphai [`numpy.ndarray`, optional] array of shape `(comps,)` Initial guess for the alphas. Defaults to -0.7.

I0i [`numpy.ndarray`, optional] array of shape `(comps,)` Initial guess for the intensities at the reference frequency. Defaults to 1.0.

tol [float, optional] Solver absolute tolerance (optional). Defaults to 1e-6.

maxiter [int, optional] Solver maximum iterations (optional). Defaults to 100.

dtype [`np.dtype`, optional] Datatype of result. Should be either `np.float32` or `np.float64`. Defaults to `np.float64`.

Returns

out [`numpy.ndarray`] array of shape `(4, comps)` The fitted components arranged as [alphas, alphavars, I0s, I0vars]

Dask

<code>fit_spi_components</code>	(data, weights, freqs, freq0)	Computes the spectral indices and the intensity at the reference frequency of a spectral index model:
---------------------------------	-------------------------------	---

`africanus.model.spi.dask.fit_spi_components` (data, weights, freqs, freq0, alphai=None, I0i=None, tol=1e-06, maxiter=100, dtype=<type 'numpy.float64'>)

Computes the spectral indices and the intensity at the reference frequency of a spectral index model:

$$I(\nu) = I(\nu_0) \left(\frac{\nu}{\nu_0} \right)^\alpha$$

Parameters

data [`dask.array.Array`] array of shape `(comps, chan)` The noisy data as a function of frequency.

weights [`dask.array.Array`] array of shape `(chan,)` Inverse of variance on each frequency axis.

freqs [`dask.array.Array`] frequencies of shape `(chan,)`

freq0 [float] Reference frequency

alphai [`dask.array.Array`, optional] array of shape `(comps,)` Initial guess for the alphas. Defaults to -0.7.

I0i [`dask.array.Array`, optional] array of shape `(comps,)` Initial guess for the intensities at the reference frequency. Defaults to 1.0.

tol [float, optional] Solver absolute tolerance (optional). Defaults to 1e-6.

maxiter [int, optional] Solver maximum iterations (optional). Defaults to 100.

dtype [`np.dtype`, optional] Datatype of result. Should be either `np.float32` or `np.float64`. Defaults to `np.float64`.

Returns

out [dask.array.Array] array of shape (4, comps) The fitted components arranged as [alphas, alphavars, I0s, I0vars]

5.7.4 Source Morphology

Shape functions for different Source Morphologies

Numpy

<code>gaussian(uvw, frequency, shape_params)</code>	Computes the Gaussian Shape Function.
---	---------------------------------------

`africanus.model.shape.gaussian(uvw, frequency, shape_params)`
Computes the Gaussian Shape Function.

$$\begin{aligned}\lambda' &= 2\lambda\pi \\ r &= \frac{e_{min}}{e_{maj}} \\ u_1 &= (u e_{maj} \cos(\alpha) - v e_{maj} \sin(\alpha)) r \lambda' \\ v_1 &= (u e_{maj} \sin(\alpha) - v e_{maj} \cos(\alpha)) \lambda' \\ \text{shape} &= e^{(-u_1^2 - v_1^2)}\end{aligned}$$

where:

- u and v are the UV coordinates and λ the frequency.
- e_{maj} and e_{min} are the major and minor axes and α the position angle.

Parameters

uvw [numpy.ndarray] UVW coordinates of shape (row, 3)

frequency [numpy.ndarray] frequencies of shape (chan,)

shape_param [numpy.ndarray] Gaussian Shape Parameters of shape (source, 3)
where the second dimension contains the (*emajor*, *eminor*, *angle*) parameters describing the shape of the Gaussian

Returns

gauss_shape [numpy.ndarray] Shape parameters of shape (source, row, chan)

Dask

<code>gaussian(uvw, frequency, shape_params)</code>	Computes the Gaussian Shape Function.
---	---------------------------------------

`africanus.model.shape.dask.gaussian(uvw, frequency, shape_params)`
 Computes the Gaussian Shape Function.

$$\begin{aligned}\lambda' &= 2\lambda\pi \\ r &= \frac{e_{min}}{e_{maj}} \\ u_1 &= (u e_{maj} \cos(\alpha) - v e_{maj} \sin(\alpha)) r \lambda' \\ v_1 &= (u e_{maj} \sin(\alpha) + v e_{maj} \cos(\alpha)) r \lambda' \\ \text{shape} &= e^{(-u_1^2 - v_1^2)}\end{aligned}$$

where:

- u and v are the UV coordinates and λ the frequency.
- e_{maj} and e_{min} are the major and minor axes and α the position angle.

Parameters

uvw [`dask.array.Array`] UVW coordinates of shape (row, 3)

frequency [`dask.array.Array`] frequencies of shape (chan,)

shape_param [`dask.array.Array`] Gaussian Shape Parameters of shape (source, 3)
 where the second dimension contains the (*emajor*, *eminor*, *angle*) parameters describing the shape of the Gaussian

Returns

gauss_shape [`dask.array.Array`] Shape parameters of shape (source, row, chan)

5.7.5 WSClean Spectral Model

Utilities for creating a spectral model from a wsclean component file.

Numpy

<code>load(filename)</code>	Loads wsclean component model.
<code>spectra(I, coeffs, log_poly, ref_freq, frequency)</code>	Produces a spectral model from a polynomial expansion of a wsclean file model.

`africanus.model.wsclean.load(filename)`
 Loads wsclean component model.

```
sources = load("components.txt")
sources = dict(sources) # Convert to dictionary

I = sources["I"]
ref_freq = sources["ReferenceFrequency"]
```

See the [WSClean Component List](#) for further details.

Parameters

filename [str or iterable] Filename of wsclean model file or iterable producing the lines of the file.

Returns

list of (name, list of values) tuples list of column (name, value) tuples

See also:

`africanus.model.wsclean.spectra`

`africanus.model.wsclean.spectra` (*I*, *coeffs*, *log_poly*, *ref_freq*, *frequency*)

Produces a spectral model from a polynomial expansion of a wsclean file model. Depending on how *log_poly* is set ordinary or logarithmic polynomials are used to produce the expansion:

$$flux(\lambda) = I_0 + \sum_{c=0} coeffs(c)(\lambda/\lambda_{ref} - 1)^{c+1}$$

$$flux(\lambda) = \exp \left(\log I_0 + \sum_{c=0} coeffs(c) \log(\lambda/\lambda_{ref})^{c+1} \right)$$

See the [WSClean Component List](#) for further details.

Parameters

I [`numpy.ndarray`] flux density in Janskys at the reference frequency of shape (*source*,)

coeffs [`numpy.ndarray`] Polynomial coefficients for each source of shape (*source*, *comp*)

log_poly [`numpy.ndarray` or `bool`] boolean array of shape (*source*,) indicating whether logarithmic (`True`) or ordinary (`False`) polynomials should be used.

ref_freq [`numpy.ndarray`] Source reference frequencies of shape (*source*,)

frequency [`numpy.ndarray`] frequencies of shape (*chan*,)

Returns

spectral_model [`numpy.ndarray`] Spectral Model of shape (*source*, *chan*)

See also:

`africanus.model.wsclean.load`

Dask

<code>spectra</code> (<i>stokes</i> , <i>spi</i> , <i>log_si</i> , <i>ref_freq</i> , <i>frequency</i>)	Produces a spectral model from a polynomial expansion of a wsclean file model.
--	--

`africanus.model.wsclean.dask.spectra` (*stokes*, *spi*, *log_si*, *ref_freq*, *frequency*)

Produces a spectral model from a polynomial expansion of a wsclean file model. Depending on how *log_poly* is set ordinary or logarithmic polynomials are used to produce the expansion:

$$flux(\lambda) = I_0 + \sum_{c=0} coeffs(c)(\lambda/\lambda_{ref} - 1)^{c+1}$$

$$flux(\lambda) = \exp \left(\log I_0 + \sum_{c=0} coeffs(c) \log(\lambda/\lambda_{ref})^{c+1} \right)$$

See the [WSClean Component List](#) for further details.

Parameters

I [`dask.array.Array`] flux density in Janskys at the reference frequency of shape

(source,)

coeffs [dask.array.Array] Polynomial coefficients for each source of shape (source, comp)

log_poly [dask.array.Array or bool] boolean array of shape (source,) indicating whether logarithmic (True) or ordinary (False) polynomials should be used.

ref_freq [dask.array.Array] Source reference frequencies of shape (source,)

frequency [dask.array.Array] frequencies of shape (chan,)

Returns

spectral_model [dask.array.Array] Spectral Model of shape (source, chan)

See also:

`africanus.model.wsclean.load`

5.8 Averaging

Routines for averaging visibility data.

5.8.1 Time and Channel Averaging

The routines in this section average row-based samples by:

1. Averaging samples of consecutive **time** values into bins defined by an period of `time_bin_secs` seconds.
2. Averaging channel data into equally sized bins of `chan_bin_size`.

In order to achieve this, a **baseline x time** ordering is established over the input data where **baseline** corresponds to the unique (ANTENNA1, ANTENNA2) pairs and **time** corresponds to the unique, monotonically increasing **TIME** values associated with the rows of a Measurement Set.

Baseline	T0	T1	T2	T3	T4
(0, 0)	0.1	0.2	0.3	0.4	0.5
(0, 1)	0.1	0.2	0.3	0.4	0.5
(0, 2)	0.1	0.2	X	0.4	0.5
(1, 1)	0.1	0.2	0.3	0.4	0.5
(1, 2)	0.1	0.2	0.3	0.4	0.5
(2, 2)	0.1	0.2	0.3	0.4	0.5

It is possible for times or baselines to be missing. In the above example, T2 is missing for baseline (0, 2).

For each baseline, adjacent time's are assigned to a bin if $h_c - h_e/2 - (l_c - l_e/2) < \text{time_bin_secs}$, where h_c and l_c are the upper and lower time and h_e and l_e are the upper and lower intervals, taken from the **INTERVAL** column. Note that no distinction is made between flagged and unflagged data when establishing the endpoints in the bin.

The reason for this is that the [Measurement Set v2.0 Specification](#) specifies that **TIME** and **INTERVAL** columns are defined as containing the *nominal* time and period at which the visibility was sampled. This means that their values include valid, flagged and missing data. Thus, averaging a regular high-resolution **baseline x htime** grid should produce a regular low-resolution **baseline x ltime** grid (**htime** > **ltime**) in the presence of bad data

By contrast, other columns such as **TIME_CENTROID** and **EXPOSURE** contain the *effective* time and period as they exclude missing and bad data. Their increased accuracy, and therefore variability means that they are unsuitable for establishing a grid over the data.

To summarise, the averaged times in each bin establish a map:

- from possibly unordered input rows.
- to a reduced set of output rows ordered by averaged `(TIME, ANTENNA1, ANTENNA2)`.

Flagged Data Handling

Both **FLAG_ROW** and **FLAG** columns may be supplied to the averager, but they should be consistent with each other. The averager will throw an exception if this is not the case, rather than making an assumption as to which is correct.

When provided with flags, the averager will output averages for bins that are completely flagged.

Part of the reason for this is that the specifies that the **TIME** and **INTERVAL** columns represent the *nominal* time and interval values. This means that they should represent valid as well as flagged or missing data in their computation.

By contrast, most other columns such as **TIME_CENTROID** and **EXPOSURE**, contain the *effective* values and should only include valid, unflagged data.

To support this:

1. **TIME** and **INTERVAL** are averaged using both flagged and unflagged samples.
2. Other columns, such as **TIME_CENTROID** are handled as follows:
 1. If the bin contains some unflagged data, only this data is used to calculate average.
 2. If the bin is completely flagged, the average of all samples (which are all flagged) will be used.
3. In both cases, a completely flagged bin will have it's flag set.
4. To support the two cases, twice the memory of the output array is required to track both averages, but only one array of merged values is returned.

Guarantees

1. Averaged output data will be lexicographically ordered by `(TIME, ANTENNA1, ANTENNA2)`
2. **TIME** and **INTERVAL** columns always contain the *nominal* average and sum and therefore contain both and missing or unflagged data.
3. Other columns will contain the *effective* average and will contain only valid data *except* when all data in the bin is flagged.
4. Completely flagged bins will be set as flagged in both the *nominal* and *effective* case.
5. Certain columns are averaged, while others are summed, or simply assigned to the last value in the bin in the case of antenna indices.
6. **Visibility data** is averaged by multiplying and dividing by **WEIGHT_SPECTRUM** or **WEIGHT** or natural weighting, in order of priority.

$$\frac{\sum v_i w_i}{\sum w_i}$$

7. **SIGMA_SPECTRUM** is averaged by multiplying and dividing by **WEIGHT_SPECTRUM** or **WEIGHT** or natural weighting, in order of priority and availability.

SIGMA is only averaged with **WEIGHT** or natural weighting.

$$\sqrt{\frac{\sum w_i^2 \sigma_i^2}{(\sum w_i)^2}}$$

Column	Unflagged/Flagged sample handling	Aggregation Method	Required
TIME	Nominal	Mean	Yes
INTERVAL	Nominal	Sum	Yes
ANTENNA1	Nominal	Assigned to Last Input	Yes
ANTENNA2	Nominal	Assigned to Last Input	Yes
TIME_CENTROID	Effective	Mean	No
EXPOSURE	Effective	Sum	No
FLAG_ROW	Effective	Set if All Inputs Flagged	No
UVW	Effective	Mean	No
WEIGHT	Effective	Sum	No
SIGMA	Effective	Weighted Mean	No
CHAN_FREQ	Nominal	Mean	No
CHAN_WIDTH	Nominal	Sum	No
DATA (vis)	Effective	Weighted Mean	No
FLAG	Effective	Set if All Inputs Flagged	No
WEIGHT_SPECTRUM	Effective	Sum	No
SIGMA_SPECTRUM	Effective	Weighted Mean	No

Dask Implementation

The dask implementation chunks data up by row and channel and averages each chunk independently of values in other chunks. This should be kept in mind if one wishes to maintain a particular ordering in the output dask arrays.

Typically, Measurement Set data is monotonically ordered in time. To maintain this guarantee in output dask arrays, the chunks will need to be separated by distinct time values. Practically speaking this means that the first and second chunk should not both contain value time 0.1, for example.

Numpy

`time_and_channel`(time, interval, antenna1, ...) Averages in time and channel.

```
africanus.averaging.time_and_channel (time,          interval,          antenna1,          antenna2,
                                     time_centroid=None,          exposure=None,
                                     flag_row=None,          uvw=None,          weight=None,
                                     sigma=None, chan_freq=None, chan_width=None,
                                     vis=None, flag=None, weight_spectrum=None,
                                     sigma_spectrum=None,          time_bin_secs=1.0,
                                     chan_bin_size=1)
```

Averages in time and channel.

Parameters

time [numpy.ndarray] Time values of shape (row,).

interval [numpy.ndarray] Interval values of shape (row,).

antenna1 [numpy.ndarray] First antenna indices of shape (row,)

antenna2 [`numpy.ndarray`] Second antenna indices of shape `(row,)`

time_centroid [`numpy.ndarray`, optional] Time centroid values of shape `(row,)`

exposure [`numpy.ndarray`, optional] Exposure values of shape `(row,)`

flag_row [`numpy.ndarray`, optional] Flagged rows of shape `(row,)`.

uvw [`numpy.ndarray`, optional] UVW coordinates of shape `(row, 3)`.

weight [`numpy.ndarray`, optional] Weight values of shape `(row, corr)`.

sigma [`numpy.ndarray`, optional] Sigma values of shape `(row, corr)`.

chan_freq [`numpy.ndarray`, optional] Channel frequencies of shape `(chan,)`.

chan_width [`numpy.ndarray`, optional] Channel widths of shape `(chan,)`.

vis [`numpy.ndarray`, optional] Visibility data of shape `(row, chan, corr)`.

flag [`numpy.ndarray`, optional] Flag data of shape `(row, chan, corr)`.

weight_spectrum [`numpy.ndarray`, optional] Weight spectrum of shape `(row, chan, corr)`.

sigma_spectrum [`numpy.ndarray`, optional] Sigma spectrum of shape `(row, chan, corr)`.

time_bin_secs [`float`, optional] Maximum summed interval in seconds to include within a bin. Defaults to 1.0.

chan_bin_size [`int`, optional] Number of bins to average together. Defaults to 1.

Returns

namedtuple A namedtuple whose entries correspond to the input arrays. Output arrays will generally be `None` if the inputs were `None`.

Dask

<code>time_and_channel</code> (time, interval, antenna1, ...)	Averages in time and channel.
---	-------------------------------

```
africanus.averaging.dask.time_and_channel(time, interval, antenna1, antenna2,
                                           time_centroid=None, exposure=None,
                                           flag_row=None, uvw=None, weight=None,
                                           sigma=None, chan_freq=None,
                                           chan_width=None, vis=None,
                                           flag=None, weight_spectrum=None,
                                           sigma_spectrum=None, time_bin_secs=1.0,
                                           chan_bin_size=1)
```

Averages in time and channel.

Parameters

time [`dask.array.Array`] Time values of shape `(row,)`.

interval [`dask.array.Array`] Interval values of shape `(row,)`.

antenna1 [`dask.array.Array`] First antenna indices of shape `(row,)`

antenna2 [`dask.array.Array`] Second antenna indices of shape `(row,)`

time_centroid [`dask.array.Array`, optional] Time centroid values of shape `(row,)`

exposure [dask.array.Array, optional] Exposure values of shape (row,).

flag_row [dask.array.Array, optional] Flagged rows of shape (row,).

uvw [dask.array.Array, optional] UVW coordinates of shape (row, 3).

weight [dask.array.Array, optional] Weight values of shape (row, corr).

sigma [dask.array.Array, optional] Sigma values of shape (row, corr).

chan_freq [dask.array.Array, optional] Channel frequencies of shape (chan,).

chan_width [dask.array.Array, optional] Channel widths of shape (chan,).

vis [dask.array.Array, optional] Visibility data of shape (row, chan, corr).

flag [dask.array.Array, optional] Flag data of shape (row, chan, corr).

weight_spectrum [dask.array.Array, optional] Weight spectrum of shape (row, chan, corr).

sigma_spectrum [dask.array.Array, optional] Sigma spectrum of shape (row, chan, corr).

time_bin_secs [float, optional] Maximum summed interval in seconds to include within a bin. Defaults to 1.0.

chan_bin_size [int, optional] Number of bins to average together. Defaults to 1.

Returns

namedtuple A namedtuple whose entries correspond to the input arrays. Output arrays will generally be None if the inputs were None.

5.9 Utilities

5.9.1 Command Line

<code>parse_python_assigns(assign_str)</code>	Parses a string, containing assign statements into a dictionary.
---	--

`africanus.util.cmdline.parse_python_assigns(assign_str)`

Parses a string, containing assign statements into a dictionary.

```
data = parse_python_assigns("beta=5.6; l=[2,3], s='hello, world'")

assert data == {
    'beta': 5.6,
    'l': [2, 3],
    's': 'hello, world'
}
```

Parameters

assign_str: str Assignment string. Should only contain assignment statements assigning python literals or builtin function calls, to variable names. Multiple assignment statements should be separated by semi-colons.

Returns

dict Dictionary { name: value } containing assignment results.

5.9.2 Requirements Handling

<code>requires_optional(*requirements)</code>	Decorator returning either the original function, or a dummy function raising a <code>MissingPackageException</code> when called, depending on whether the supplied requirements are present.
---	---

`africanus.util.requirements.requires_optional(*requirements)`

Decorator returning either the original function, or a dummy function raising a `MissingPackageException` when called, depending on whether the supplied requirements are present.

If packages are missing and called within a test, the dummy function will call `pytest.skip()`.

Used in the following way:

```
try:
    from scipy import interpolate
except ImportError as e:
    # https://stackoverflow.com/a/29268974/1611416, pep 3110 and 344
    scipy_import_error = e
else:
    scipy_import_error = None

@requires_optional('scipy', scipy_import_error)
def function(*args, **kwargs):
    return interpolate(...)
```

Parameters

requirements [iterable of string, None or ImportError] Sequence of package names required by the decorated function. `ImportError` exceptions (or None, indicating their absence) may also be supplied and will be immediately re-raised within the decorator. This is useful for tracking down problems in user import logic.

Returns

callable Either the original function if all requirements are available or a dummy function that throws a `MissingPackageException` or skips a `pytest`.

5.9.3 Shapes

<code>aggregate_chunks(chunks, max_chunks)</code>	Aggregate dask chunks together into chunks no larger than <code>max_chunks</code> .
<code>corr_shape(ncorr, corr_shape)</code>	Returns the shape of the correlations, given <code>ncorr</code> and the type of correlation shape requested

`africanus.util.shapes.aggregate_chunks(chunks, max_chunks)`

Aggregate dask chunks together into chunks no larger than `max_chunks`.

```
chunks, max_c = ((3,4,6,3,6,7), (1,1,1,1,1,1)), (10,3)
expected = ((7,9,6,7), (2,2,1,1))
assert aggregate_chunks(chunks, max_c) == expected
```

Parameters

chunks [sequence of tuples or tuple]
max_chunks [sequence of ints or int]

Returns

sequence of tuples or tuple

`africanus.util.shapes.corr_shape(ncorr, corr_shape)`

Returns the shape of the correlations, given `ncorr` and the type of correlation shape requested

Parameters

ncorr [integer] Number of correlations
corr_shape [{ 'flat', 'matrix' }] Shape of output correlations

Returns

tuple Shape tuple describing the correlation dimensions

- If `flat` returns `(ncorr,)`
- If `matrix` returns
 - `(1,)` if `ncorr == 1`
 - `(2,)` if `ncorr == 2`
 - `(2,2)` if `ncorr == 4`

5.9.4 Beams

<code>beam_filenames(filename_schema, ...)</code>	Returns a dictionary of beam filename pairs, keyed on correlation, from the cartesian product of correlations and real, imaginary pairs
<code>beam_grids(header)</code>	Extracts the FITS indices and grids for the beam dimensions in the supplied FITS header.

`africanus.util.beams.beam_filenames(filename_schema, polarisation_type)`

Returns a dictionary of beam filename pairs, keyed on correlation, from the cartesian product of correlations and real, imaginary pairs

Given `beam_${corr}_${reim}.fits` returns:

```
{
  'xx' : ('beam_xx_re.fits', 'beam_xx_im.fits'),
  'xy' : ('beam_xy_re.fits', 'beam_xy_im.fits'),
  ...
  'yy' : ('beam_yy_re.fits', 'beam_yy_im.fits'),
}
```

Given `beam_${CORR}_${REIM}.fits` returns:

```
{
  'xx' : ('beam_XX_RE.fits', 'beam_XX_IM.fits'),
  'xy' : ('beam_XY_RE.fits', 'beam_XY_IM.fits'),
  ...
  'yy' : ('beam_YY_RE.fits', 'beam_YY_IM.fits'),
}
```

Parameters

filename_schema [str] String containing the filename schema.

polarisation_type [{‘linear’, ‘circular’}] String defining the type of polarisation.

Returns

dict Dictionary of schema {**correlation** : (refile, imfile)} mapping correlations to real and imaginary filename pairs

`africanus.util.beams.beam_grids(header)`

Extracts the FITS indices and grids for the beam dimensions in the supplied FITS `header`. Specifically the axes specified by

1. L or X CTYPE
2. M or Y CTYPE
3. FREQ CTYPE

If the first two axes have a negative sign, such as `-L`, the grid will be inverted.

Any grids corresponding to axes with a CUNIT type of `DEG` will be converted to radians.

Parameters

header [Header or dict] FITS header object.

Returns

tuple Returns ((l_axis, l_grid), (m_axis, m_grid), (freq_axis, freq_grid)) where the axis is the FORTRAN indexed FITS axis (1-indexed) and grid contains the values at each pixel along the axis.

5.9.5 Code

<code>format_code(code)</code>	Formats some code with line numbers
<code>memoize_on_key(key_fn)</code>	Memoize based on a key function supplied by the user.

`africanus.util.code.format_code(code)`

Formats some code with line numbers

Parameters

code [str] Code

Returns

str Code prefixed with line numbers

`class africanus.util.code.memoize_on_key(key_fn)`

Memoize based on a key function supplied by the user. The key function should return a custom key for

memoizing the decorated function, based on the arguments passed to it.

In the following example, the arguments required to generate the `_generate_phase_delay_kernel` function are the types of the `lm`, `uvw` and `frequency` arrays, as well as the number of correlations, `ncorr`.

The supplied `key_fn` produces a unique key based on these types and the number of correlations, which is used to cache the generated function.

```
def key_fn(lm, uvw, frequency, ncorrs=4):
    '''
    Produce a unique key for the arguments of
    _generate_phase_delay_kernel
    '''
    return (lm.dtype, uvw.dtype, frequency.dtype, ncorrs)

_code_template = jinja2.Template('''
#define ncorrs {{ncorrs}}

__global__ void phase_delay(
    const {{lm_type}} * lm,
    const {{uvw_type}} * uvw,
    const {{freq_type}} * frequency,
    {{out_type}} * out)
{
    ...
}
''')

_type_map = {
    np.float32: 'float',
    np.float64: 'double'
}

@memoize_on_key(key_fn)
def _generate_phase_delay_kernel(lm, uvw, frequency, ncorrs=4):
    ''' Generate the phase delay kernel '''
    out_dtype = np.result_type(lm.dtype, uvw.dtype, frequency.dtype)
    code = _code_template.render(lm_type=_type_map[lm.dtype],
                                uvw_type=_type_map[uvw.dtype],
                                freq_type=_type_map[frequency.dtype],
                                ncorrs=ncorrs)
    return cp.RawKernel(code, "phase_delay")
```

Methods

<code>__call__</code>	
-----------------------	--

5.9.6 CUDA

`grids(dims, blocks)`

Determine the grid size, given space dimensions sizes and blocks

`africanus.util.cuda.grids(dims, blocks)`

Determine the grid size, given space dimensions sizes and blocks

Parameters

dims [tuple of ints] (x, y, z) tuple

Returns

tuple (x, y, z) grid size tuple

Contributions are welcome, and they are greatly appreciated! Every little bit helps, and credit will always be given. You can contribute in many ways:

6.1 Types of Contributions

6.1.1 Report Bugs

Report bugs at <https://github.com/ska-sa/codex-africanus/issues>.

If you are reporting a bug, please include:

- Your operating system name and version.
- Any details about your local setup that might be helpful in troubleshooting.
- Detailed steps to reproduce the bug.

6.1.2 Fix Bugs

Look through the GitHub issues for bugs. Anything tagged with “bug” and “help wanted” is open to whoever wants to implement it.

6.1.3 Implement Features

Look through the GitHub issues for features. Anything tagged with “enhancement” and “help wanted” is open to whoever wants to implement it.

6.1.4 Write Documentation

Codex Africanus could always use more documentation, whether as part of the official Codex Africanus docs, in docstrings, or even on the web in blog posts, articles, and such.

6.1.5 Submit Feedback

The best way to send feedback is to file an issue at <https://github.com/ska-sa/codex-africanus/issues>.

If you are proposing a feature:

- Explain in detail how it would work.
- Keep the scope as narrow as possible, to make it easier to implement.
- Remember that this is a volunteer-driven project, and that contributions are welcome :)

6.2 Get Started!

Ready to contribute? Here's how to set up *codex-africanus* for local development.

1. Fork the *codex-africanus* repo on GitHub.
2. Clone your fork locally:

```
$ git clone git@github.com:your_name_here/codex-africanus.git
```

3. Install your local copy into a virtualenv. Assuming you have virtualenvwrapper installed, this is how you set up your fork for local development:

```
$ mkvirtualenv codex-africanus
$ cd codex-africanus/
$ pip install -e .
```

4. Create a branch for local development:

```
$ git checkout -b name-of-your-bugfix-or-feature
```

Now you can make your changes locally.

5. When you're done making changes, check that your changes pass the test cases, fixup your PEP8 compliance, and check for any code style issues:

```
$ py.test -v africanus $ autopep8 -r -i africanus $ flake8 africanus $ pycodestyle africanus
```

To get autopep8 and pycodestyle, just pip install them into your virtualenv.

6. Commit your changes and push your branch to GitHub:

```
$ git add .
$ git commit -m "Your detailed description of your changes."
$ git push origin name-of-your-bugfix-or-feature
```

7. Submit a pull request through the GitHub website.

6.3 Pull Request Guidelines

Before you submit a pull request, check that it meets these guidelines:

1. The pull request should include tests.
2. If the pull request adds functionality, the docs should be updated. Put your new functionality into a function with a docstring, and add the feature to the list in HISTORY.rst.
3. The pull request should work for Python 2.7, 3.5 and 3.6. Check https://travis-ci.org/ska-sa/codex-africanus/pull_requests and make sure that the tests pass for all supported Python versions.

6.4 Tips

To run a subset of tests:

```
$ py.test tests.test_africanus
```

6.5 Deploying

A reminder for the maintainers on how to deploy.

1. Start a release branch


```
$ git checkout -b prepare-release-Z.Y.X.
```
2. Update HISTORY.rst with the intended release number Z.Y.X and commit to git.
3. Bump the version number. If your current version is Z.Y.W and the new version is Z.Y.X call:

```
$ python -m pip install bumpversion
$ bumpversion --current-version Z.Y.W --new-version Z.Y.X patch
```

4. Push the release branch to github and merge it.

```
$ git push origin prepare-release-Z.Y.X
```

5. Create the source and wheel distributions:

```
$ git checkout master
$ git pull origin master
$ python setup.py sdist bdist_wheel
```

6. Install twine and upload the source distribution to the pypi **test** server. Here, **pypitest** refers to the pypi test server setup in a .pypirc file.:

```
$ python -m pip install twine
$ python -m twine upload -r pypitest dist/codex-africanus-Z.Y.X.tar.gz
```

7. Test pypi install on different python versions, running the test cases.

```
$ python -m virtualenv --python=pythonM.N test
$ source test/bin/activate
(test) $ pip install --index-url https://test.pypi.org/simple --extra-index-url_
↪https://pypi.org/simple codex-africanus[complete]==Z.Y.X
(test) $ py.test /path/to/tests
```

8. Upload the source distribution to the main pypi server. Here, **pypi** refers to the main pypi setup in a `.pypirc` file.:

```
$ python -m twine upload -r pypi dist/codex-africanus-Z.Y.X*
```

9. Tag the release commit, push the release commits and tag to github.:

```
$ git tag Z.Y.X
$ git push
$ git push --tags
```

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8.1 0.1.6 (YYYY-MM-DD)

8.2 0.1.5 (2019-05-09)

- Predict script enhancements ([GH#103](#)) and dask channel chunking fix ([GH#104](#)).
- Directly jit DFT functions ([GH#100](#), [GH#101](#))
- Spectral Models ([GH#86](#))
- Fix radec sign conversion in wsclean sky model ([GH#96](#))
- Full Time and Channel Averaging Implementation ([GH#80](#), [GH#97](#), [GH#98](#))
- Support integer seconds in wsclean ra and dec columns ([GH#91](#), [GH#93](#))
- Fix ratio computation in Gaussian Shape ([GH#89](#), [GH#90](#))

8.3 0.1.4 (2019-03-11)

- Support *complete* and *complete-cuda* to support non-GPU installs ([GH#87](#))
- Gaussian Shape Parameter Implementation ([GH#82](#), [GH#83](#))
- WSClean Spectral Model ([GH#81](#))
- Compare predict versus MeqTrees ([GH#79](#))
- Time and channel averaging ([GH#75](#))
- cupy implementation of *predict_vis* ([GH#73](#))
- Introduce transpose in second antenna term of predict ([GH#72](#))
- cupy implementation of *feed_rotation* ([GH#67](#))

- cupy implementation of *stokes_convert* kernel (GH#65)
- Add a basic RIME example (GH#64)
- *requires_optional* accepts ImportError's for a better debugging experience (GH#62, GH#63)
- Added *fit_component_spi* function (GH#61)
- cupy implementation of the *phase_delay* kernel (GH#59)
- Correct *phase_delay* argument ordering (GH#57)
- Support dask for *radec_to_lmn* and *lmn_to_radec*. Also add support for *radec_to_lm* and *lm_to_radec* (GH#56)
- Added test for dft to test if image space covariance is symmetric (GH#55)
- Correct Parallactic Angle Computation (GH#49)
- Enhance visibility predict (GH#50)
- Fix Kaiser Bessel filter and taper (GH#48)
- Stokes/Correlation conversion (GH#41)
- Fix gridding examples (GH#43)
- Add simple dask gridder example (GH#42)
- Implement Kaiser Bessel filter (GH#38)
- Implement W-stacking gridder/degridder (GH#38)
- Use 2D filters by default (GH#37)
- Fixed bug in *im_to_vis*. Added more tests for *im_to_vis*. Removed division by *n* since it is trivial to reinstate after the fact. (GH#34)
- Move numba implementations out of API functions. (GH#33)
- Zernike Polynomial Direction Dependent Effects (GH#18, GH#30)
- Added division by *n* to DFT. Fixed dask chunking issue. Updated *test_vis_to_im_dask* (GH#29).
- Implement RIME visibility predict (GH#24, GH#25)
- Direct Fourier Transform (GH#19)
- Parallactic Angle computation (GH#15)
- Implement Feed Rotation term (GH#14)
- Swap gridding correlation dimensions (GH#13)
- Implement Direction Dependent Effect beam cubes (GH#12)
- Implement Brightness Matrix Calculation (GH#9)
- Implement RIME Phase Delay term (GH#8)
- Support user supplied grids (GH#7)
- Add dask wrappers to the gridder and degriider (GH#4)
- Add weights to gridder/degridder and remove PSF function (GH#2)

8.4 0.1.2 (2018-03-28)

- First release on PyPI.

CHAPTER 9

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- `modindex`
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